

A W21 × 55 with $F_y = 50$ ksi is used for the beam and loads of Fig. 10.4. Check its adequacy in shear,

MACormac
Example
10-2

$w_D = 2$ k/ft (includes beam wt)
 $w_L = 4$ k/ft

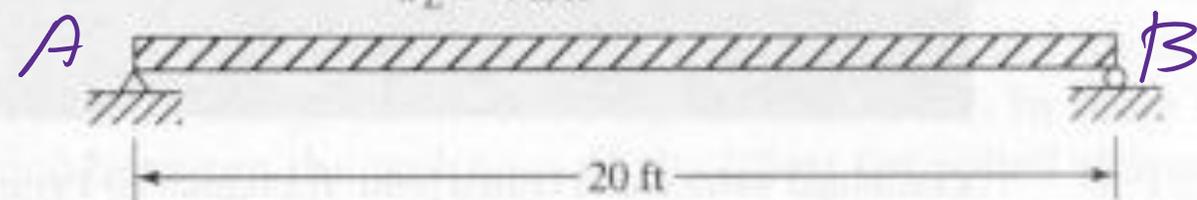


FIGURE 10.4

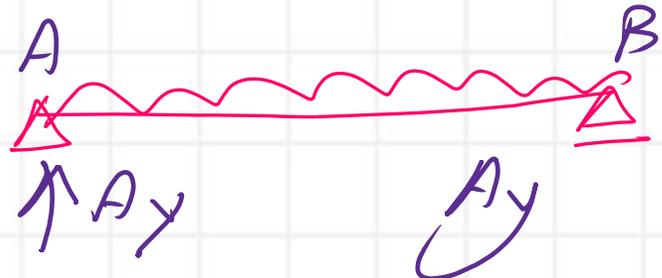
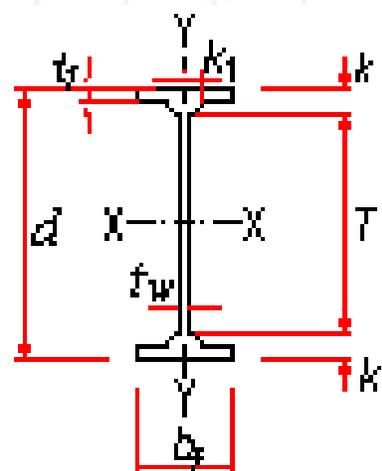
① LRFD design

$l = 20'$

$$W_{Ulf} = 1.2 w_D + 1.60 w_L$$

$$= 1.2 (2) + 1.6 (4)$$

$$= 2.4 + 6.40 = 7 \text{ k/F}$$



$$A_y = w_U \cdot \frac{L}{2} = 7 (10)$$

$$= 70 \text{ kips}$$

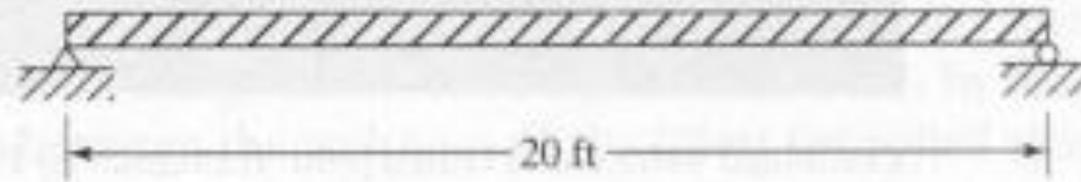
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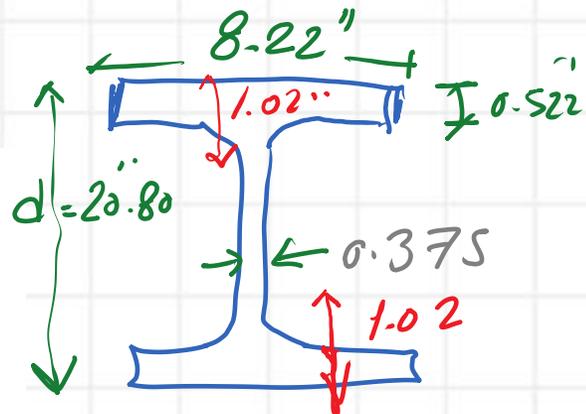
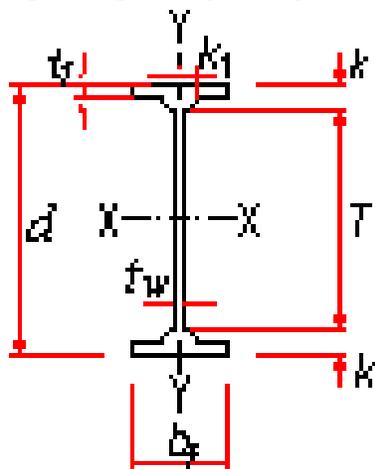
$w_D = 2$ k/ft (includes beam wt)
 $w_L = 4$ k/ft

FIGURE 10.4



Solution

W21 x 55



$$h = 20.80 - 2(1.02) = 18.76"$$

Shape	Area, A in. ²	Depth, d in.	Web		Flange		Distance								
			Thickness, t_w in.	$\frac{t_w}{2}$ in.	Width, b_f in.	Thickness, t_f in.	k		k_1 in.	T in.	Workable Gage in.				
							k_{des} in.	k_{det} in.							
W21x93	27.3	21.6	21 ⁵ / ₈	0.580	9/16	5/16	8.42	8 ³ / ₈	0.930	1 ⁵ / ₁₆	1.43	1 ⁵ / ₈	1 ⁵ / ₁₆	18 ³ / ₈	5 ¹ / ₂
x83 ^c	24.4	21.4	21 ³ / ₈	0.515	1/2	1/4	8.36	8 ³ / ₈	0.835	1 ³ / ₁₆	1.34	1 ¹ / ₂	7/8		
x73 ^c	21.5	21.2	21 ¹ / ₄	0.455	7/16	1/4	8.30	8 ¹ / ₄	0.740	3/4	1.24	1 ⁷ / ₁₆	7/8		
x68 ^c	20.0	21.1	21 ¹ / ₈	0.430	7/16	1/4	8.27	8 ¹ / ₄	0.685	1 ¹ / ₁₆	1.19	1 ³ / ₈	7/8		
x62 ^c	18.3	21.0	21	0.400	3/8	3/16	8.24	8 ¹ / ₄	0.615	5/8	1.12	1 ⁵ / ₁₆	1 ³ / ₁₆		
x55 ^c	16.2	20.8	20 ³ / ₄	0.375	3/8	3/16	8.22	8 ¹ / ₄	0.522	1/2	1.02	1 ³ / ₁₆	1 ³ / ₁₆		
x48 ^{cd}	14.1	20.6	20 ⁵ / ₈	0.350	3/8	3/16	8.14	8 ¹ / ₈	0.430	7/16	0.930	1 ¹ / ₈	1 ³ / ₁₆		

design detailing

Relation between F_y , $\frac{h}{t_w}$ for Zone I $E = 29 \times 10^6$ ksi:

$$E = 29 \times 10^6 \text{ psi} \quad \frac{h}{t_w} = 2.24 \sqrt{\frac{E}{F_y}}$$

Different Grades of steel

$$F_y = 36 \text{ ksi} \Rightarrow \frac{h}{t_w} = 2.24 \sqrt{\frac{29000}{36}} = 63.576$$

$$F_y = 42 \text{ ksi} \rightarrow \frac{h}{t_w} = 2.24 \sqrt{\frac{29000}{42}} = 58.86 \Rightarrow 58.90$$

$$F_y = 45 \text{ ksi} \rightarrow \frac{h}{t_w} = 2.24 \sqrt{\frac{29000}{45}} = 56.86 \Rightarrow 56.90$$

$$F_y = 50 \text{ ksi} \rightarrow \frac{h}{t_w} = 2.24 \left(\frac{29000}{50} \right)^{1/2} = 53.90$$

$$F_y = 60 \text{ ksi} \rightarrow \frac{h}{t_w} = 2.24 \left(\frac{29000}{60} \right)^{1/2} = 49.25$$

$$F_y = 65 \text{ ksi} \rightarrow \frac{h}{t_w} = 2.24 \left(\frac{29000}{65} \right)^{1/2} \approx 47.30$$

$$F_y = 100 \text{ ksi} \rightarrow \frac{h}{t_w} = 2.24 \left(\frac{29000}{100} \right)^{1/2} = 38.15$$

Nominal shear value

G2. I-SHAPED MEMBERS AND CHANNELS

1. Shear Strength of Webs without Tension Field Action

The nominal shear strength, V_n , is:

$$V_n = 0.6F_y A_w C_{vl} \quad (G2-1)$$

where

F_y = specified minimum yield stress of the type of steel being used, ksi (MPa)

A_w = area of web, the overall depth times the web thickness, dt_w , in.² (mm²)

$$E = 29,000$$

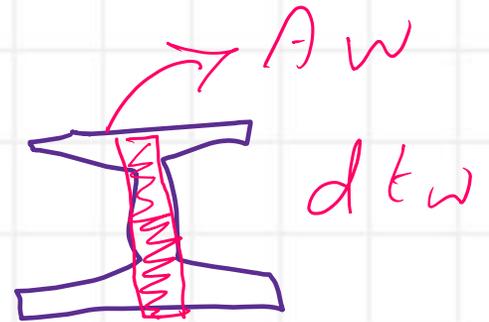
$$F_y = 50 \text{ ksi}, \quad t_w = 0.375''$$

$$h_w = 18.76''$$

$$d = 20.8''$$

$$\text{For } 2.24 \sqrt{\frac{E}{F_y}} \Rightarrow 53.90$$

$$A_w = d t_w$$



our $\frac{h}{t_w}$ For $W_{21} \times 55$ Shear stress

$$= 18.76 / 0.375 = 50.03 < 53.90$$

$$V_n = C_v t_w d (0.6 F_y) = 1 (0.375) (20.8) (0.6) (50) = 234 \text{ k}$$

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① LRFD

For G.2.1a

$$\phi = 1$$

$$\phi V_n = 1(234) = 234 \text{ kips}$$

$$V_u = 70 \text{ kips} \Rightarrow 70^k < 234^k$$

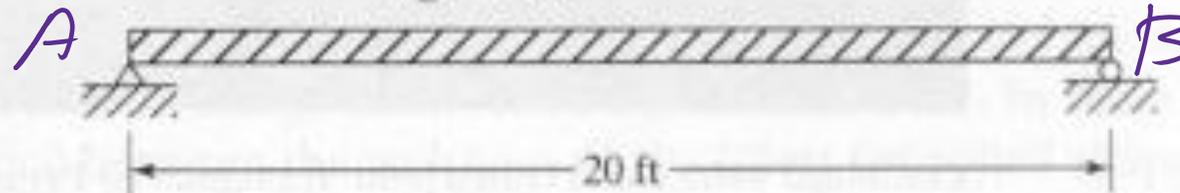
Since $V_u < \phi V_n \Rightarrow$ Section is adequate
For shear

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MACORMAC
Example
10-2

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FIGURE 10.4



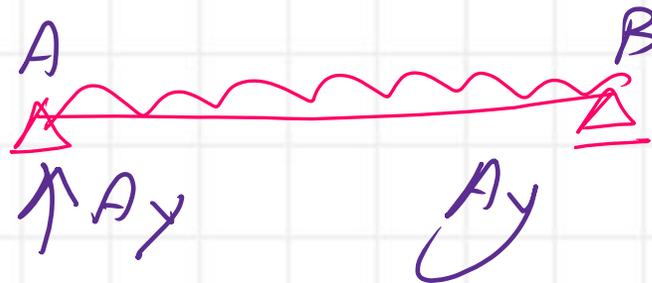
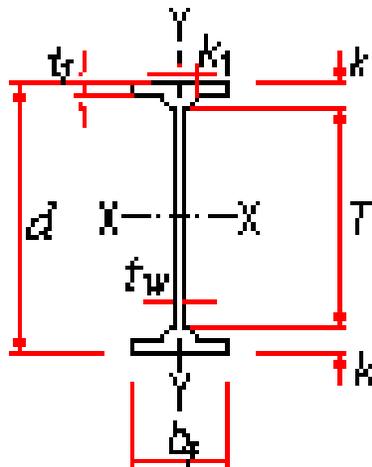
(b) ASD

design

$l = 20'$

$$W = W_D + W_L$$

$$= 2 + 4 = 6 \text{ k/ft}$$



$$A_y = W_T \cdot \frac{L}{2} = 6 (10)$$

$$= 60 \text{ kips}$$

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⑥ ASD

For G.2.1a

$$\Omega = 1.5$$

$$V_n = \frac{1}{1.5}(234) = 156 \text{ kips}$$

$$V_T = 60 \text{ kips} \Rightarrow 60 < 156$$

Since $V_T < \frac{1}{\Omega} V_n \Rightarrow$ Section is adequate
For shear

CM # 14 \Rightarrow Specification # 2010

16.1-67

CHAPTER G

DESIGN OF MEMBERS FOR SHEAR

This chapter addresses webs of singly or doubly symmetric members subject to shear in the plane of the web, single angles and *HSS* sections, and shear in the weak direction of singly or doubly symmetric shapes.

The chapter is organized as follows:

G2

- G1. General Provisions
- \rightarrow G2. Members with Unstiffened or Stiffened Webs
- G3. Tension Field Action
- G4. Single Angles
- G5. Rectangular *HSS* and Box-Shaped Members
- G6. Round *HSS*
- G7. Weak Axis Shear in Doubly Symmetric and Singly Symmetric Shapes
- G8. Beams and Girders with Web Openings

User Note: For cases not included in this chapter, the following sections apply:

- H3.3 Unsymmetric sections
- J4.2 Shear strength of connecting elements
- J10.6 Web *panel zone* shear

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16-68

MEMBERS WITH UNSTIFFENED OR STIFFENED WEBS

[Sect. G2.]

G2-1a

(a) For webs of rolled I-shaped members with $h/t_w \leq 2.24\sqrt{E/F_y}$:

$\phi_v = 1.00$
 $\Omega_v = 1.50$

and

$\phi_v = 1.00$ (LRFD) $\Omega_v = 1.50$ (ASD)

Term is C_v

$C_v = 1.0$

For $\frac{h}{t_w} \leq 2.24 \cdot \sqrt{\frac{E}{F_y}}$

(G2-2)

User Note: All current ASTM A6 W, S and HP shapes except W44×230, W40×149, W36×135, W33×118, W30×90, W24×55, W16×26 and W12×14 meet the criteria stated in Section G2.1(a) for $F_y = 50$ ksi (345 MPa).

(b) For webs of all other doubly symmetric shapes and singly symmetric shapes and channels, except round HSS, the web shear coefficient, C_v , is determined as follows:

(i) When $h/t_w \leq 1.10\sqrt{k_v E/F_y}$

$C_v = 1.0$

(G2-3)

$V_n = C_v A_w (0.6 F_y)$

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(b) For webs of all other doubly symmetric shapes and singly symmetric shapes and channels, except round *HSS*, the web shear coefficient, C_v , is determined as follows:

How to find C_v values?
when $\frac{h}{t_w}$ varies (G2-3)

(i) When $h/t_w \leq 1.10\sqrt{k_v E / F_y}$

$$C_v = 1.0$$

(ii) When $1.10\sqrt{k_v E / F_y} < h/t_w \leq 1.37\sqrt{k_v E / F_y}$

$$C_v = \frac{1.10\sqrt{k_v E / F_y}}{h/t_w} \quad (\text{G2-4})$$

(iii) When $h/t_w > 1.37\sqrt{k_v E / F_y}$

$$C_v = \frac{1.51k_v E}{(h/t_w)^2 F_y} \quad (\text{G2-5})$$

where

A_w = area of web, the overall depth times the web thickness, dt_w , in.² (mm²)

h = for rolled shapes, the clear distance between flanges less the fillet or corner radii, in. (mm)

= for built-up welded sections, the clear distance between flanges, in. (mm)

= for built-up bolted sections, the distance between *fastener* lines, in. (mm)

= for tees, the overall depth, in. (mm)

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The web plate *shear buckling* coefficient, k_v , is determined as follows:

(i) For webs without *transverse stiffeners* and with $h/t_w < 260$:

$$k_v = 5$$

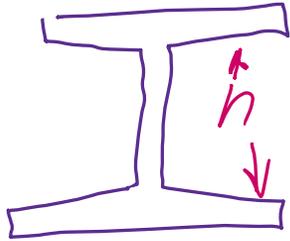
except for the stem of tee shapes where $k_v = 1.2$.

CM # 14

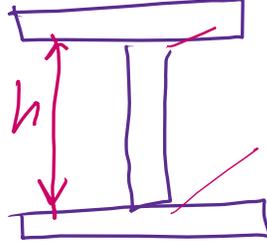
Specs - P-69

(ii) For webs with transverse stiffeners:

For
 h



clear distance
rolled



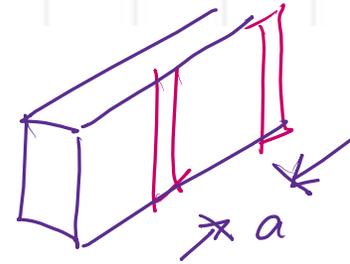
Built
up

where

a = clear distance between transverse stiffeners, in. (mm)

$$k_v = 5 + \frac{5}{(a/h)^2}$$

$$= 5 \text{ when } a/h > 3.0 \text{ or } a/h > \left[\frac{260}{(h/t_w)} \right]^2$$



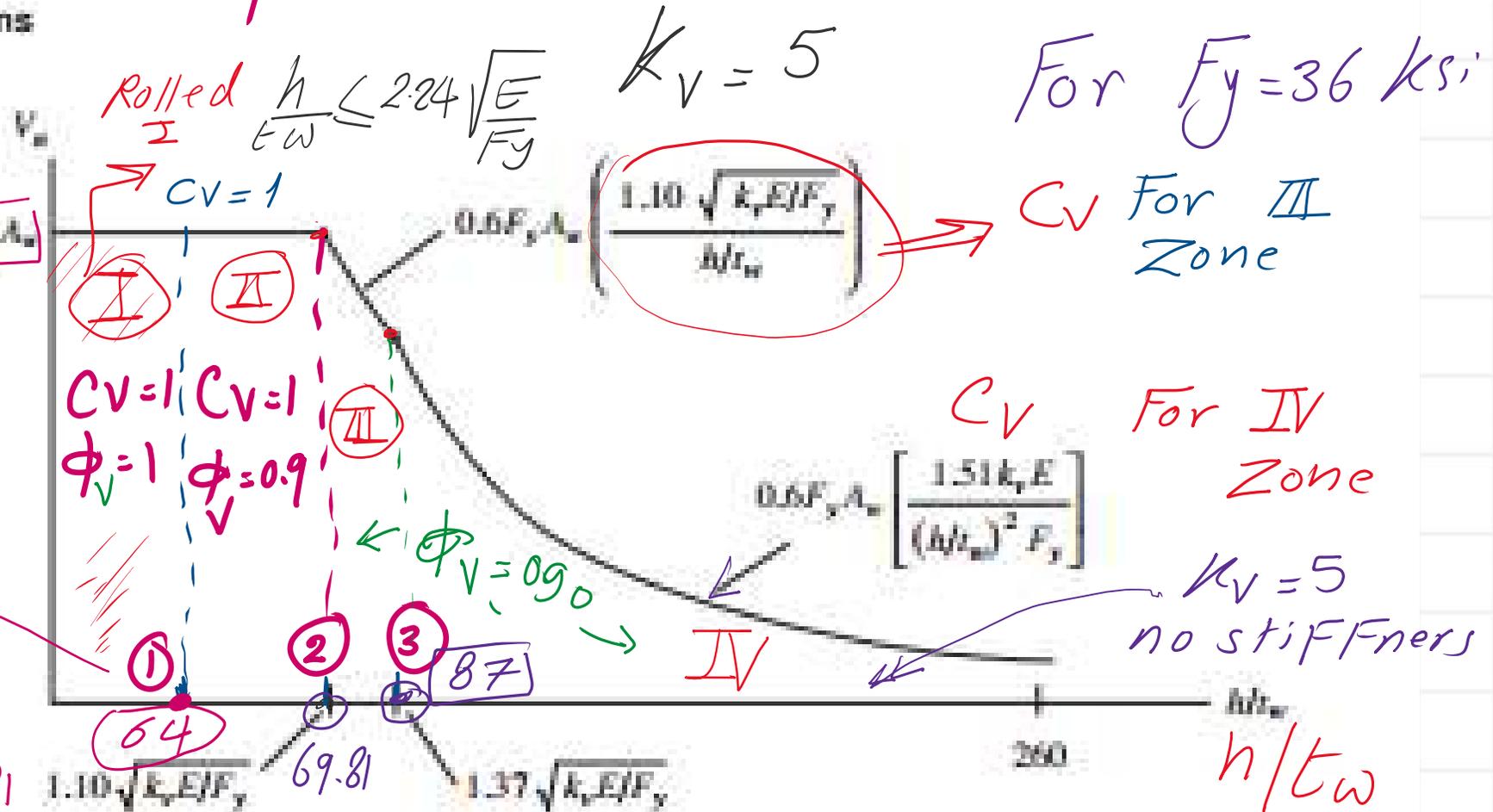
(G2-6)

User Note: For all ASTM A6 W, S, M and HP shapes except M12.5×12.4, M12.5×11.6, M12×11.8, M12×10.8, M12×10, M10×8 and M10×7.5, when $F_y = 50$ ksi (345 MPa), $C_v = 1.0$.

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FIGURE 5.19



Point # 1

$F_y = 36 \text{ ksi}$, h/t_w
 $2.24 \sqrt{\frac{E}{F_y}} = 2.24 \sqrt{\frac{29000}{36}}$
 $= 63.57$

Point . 2 : $K_v = 5$

$h/t_w = 1.1 \sqrt{\frac{K_v E}{F_y}}$
 $\frac{h}{t_w} = 1.1 \sqrt{\frac{5(29000)}{36}} = 69.81$

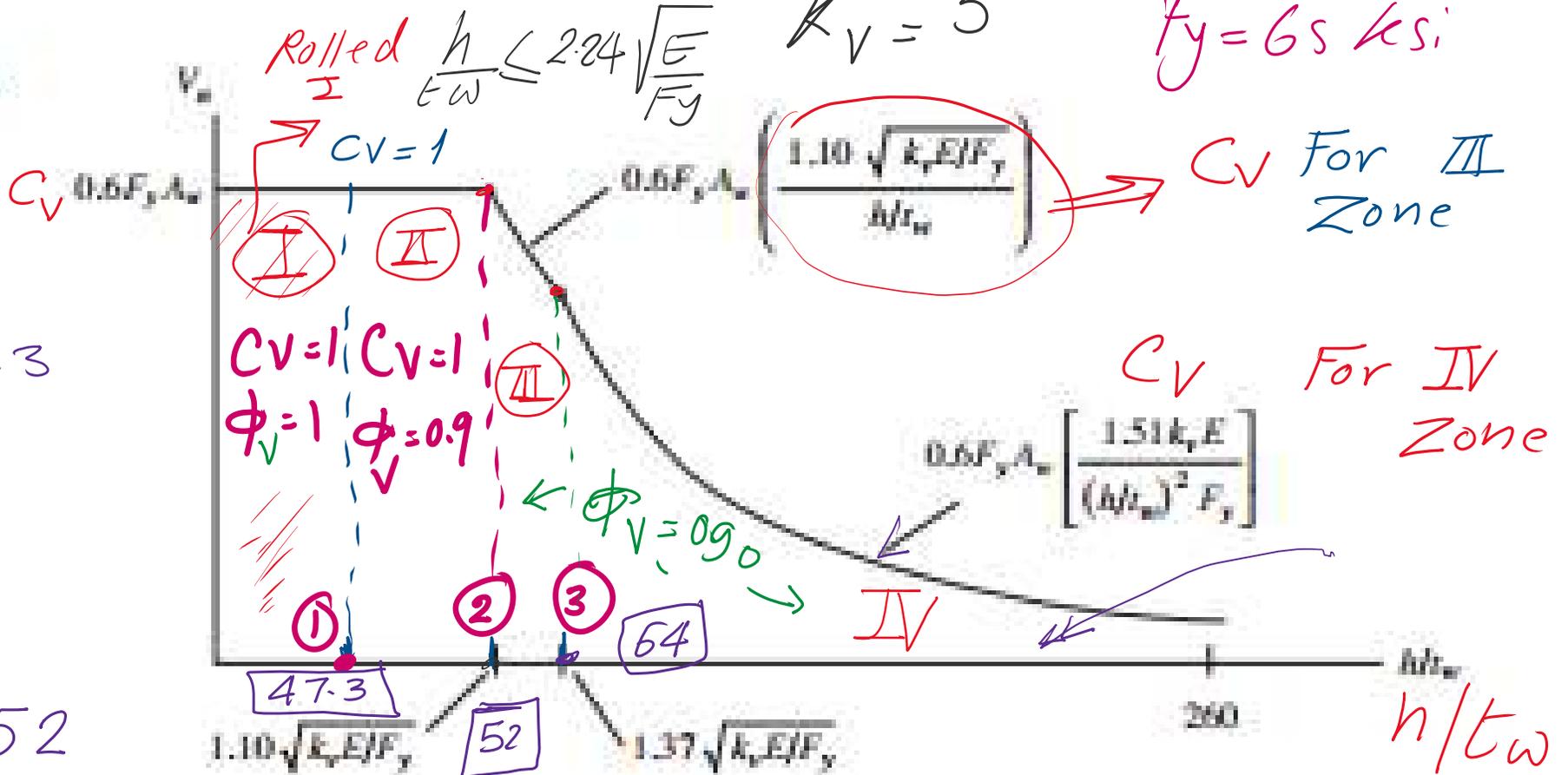
Point-3 $1.37 \sqrt{\frac{5(29000)}{36}} = 86.95 \approx 87$

$h/t_w = 1.37 \sqrt{K_v \cdot E / F_y}$

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FIGURE 5.19



Point # 1
 $F_y = 65\ ksi$

$2.24 \sqrt{\frac{E}{F_y}} = 47.3$

Point-2

$1.1 \sqrt{\frac{5(29000)}{65}} = 52$

Point-3 $1.37 \sqrt{\frac{5(29000)}{65}} \approx 64$