

*Our discussion  
For  $L_p > L_r$*

*For the  
Case  
of Elastic  
Buckling*

For  $L_b > L_r$

$$F_{cr} = \frac{C_b \pi^2 E}{(L_b/r_{ts})^2} \sqrt{1 + 0.078 \frac{Jc}{S_x h_0} \left(\frac{L_b}{r_{ts}}\right)^2}$$

In this calculation,

$$M_{cr} = F_{cr} \cdot S_x$$

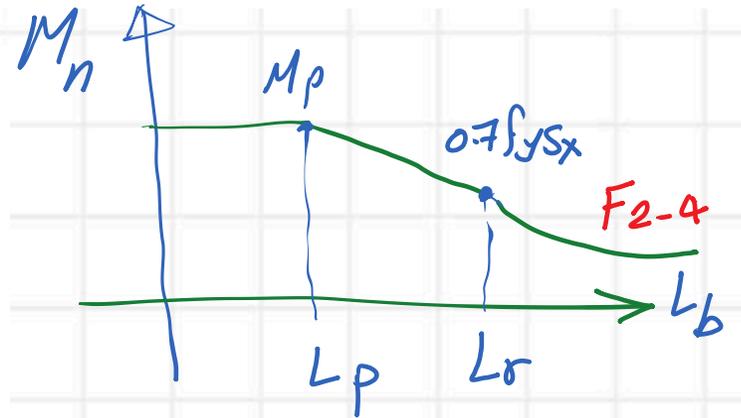
$r_{ts}$  = effective radius of gyration, in (provided in AISC Table 1-1)

$J$  = torsional constant, in<sup>4</sup> (AISC Table 1-1)

$c$  = 1.0 for doubly symmetric I-shapes

$h_0$  = distance between flange centroids, in (AISC Table 1-1)

(AISC Equation F2-4)



Example 9-7 McCormac Analysis

Using AISC Equation F2-4, determine the values of  $\phi_b M_{nx}$  and  $M_{nx}/\Omega_b$  for a W18 x 97 with  $F_y = 50$  ksi and an unbraced length  $L_b = 38$  ft. Assume that  $C_b = 1.0$ .

Solution

$F_y = 50$  ksi  
(AISC Equation F2-4)

$$F_{cr} = \frac{C_b \pi^2 E}{(L_b/r_x)^2} \sqrt{1 + 0.078 \frac{Jc}{S_x h_0} \left(\frac{L_b}{r_x}\right)^2}$$

Part - 2  
W18 x 97

Table 1-1 (continued)  
W-Shapes  
Properties



Nominal Wt. lb/ft	Compact Section Criteria		Axis X-X				Axis Y-Y				$r_x$ in.	$h_0$ in.	Torsional Properties	
	$b_f/2t_f$	$h/t_w$	$I$ in. <sup>4</sup>	$S$ in. <sup>3</sup>	$r$ in.	$Z$ in. <sup>3</sup>	$I$ in. <sup>4</sup>	$S$ in. <sup>3</sup>	$r$ in.	$Z$ in. <sup>3</sup>			$J$ in. <sup>4</sup>	$C_w$ in. <sup>6</sup>
97	6.41	30.0	1750	188	7.82	211	201	36.1	2.65	55.3	3.08	17.7	5.86	15800
86	7.20	33.4	1530	166	7.77	186	175	31.6	2.63	48.4	3.05	17.6	4.10	13600
76	8.11	37.8	1330	146	7.73	163	152	27.6	2.61	42.2	3.02	17.5	2.83	11700



$Z_x = 211$  inch<sup>3</sup>  
 $S_x = 188$  inch<sup>3</sup>

$r_{ts} = 3.08$   
 $J = 5.86$   
 $h_0 = 17.7$  inch

$C_w = 15800$  inch<sup>6</sup>  
 $r_y = 2.65$  inch

$$W_{18 \times 97} \quad F_y = 50 \text{ ksi} \Rightarrow r_y = 2.65''$$

$$L_p = \frac{300}{\sqrt{F_y}} r_y = \frac{300(2.65)}{\sqrt{50}} = 112.43''$$

$$S_x = 188 \text{ inch}^3 \quad h_o = 17.7''$$

$$\Rightarrow \frac{112.43}{12} \Rightarrow 9.3691$$

$$L_p \approx 9.37'$$

$L_r \Rightarrow$  by Estimation  
by Table 3-2

$$L_r = 1.95 r_{ts} \frac{E}{0.7 F_y} \sqrt{\frac{J_c}{S_x h_o} + \sqrt{\left(\frac{J_c}{S_x h_o}\right)^2 + 6.76 \left(\frac{0.7 F_y}{E}\right)^2}} \quad (\text{F2-6})$$

$$L_r = 1.95 (3.08) \left( \frac{29000}{0.7(50)} \right) \sqrt{\left( \frac{(5.86)(1)}{188(17.7)} \right) + \sqrt{\left( \frac{5.86}{188(17.7)} \right)^2 + 6.76 \left( \frac{(0.7)50}{29000} \right)^2}}$$

$$L_r = 364.159'' \Rightarrow /12 = 30.35' \approx 30.4'$$

Check  $L_r$  value From Table 3-2

Shape	$Z_x$ in. <sup>3</sup>	$M_{px}/\Omega_b$		$\phi_b M_{px}$		$M_{rx}/\Omega_b$		$\phi_b M_{rx}$		$L_p$ ft	$L_r$ ft	$I_x$ in. <sup>4</sup>	$V_{max}/\Omega_v$	
		kip-ft	kip-ft	kip-ft	kip-ft	kip-ft	kip-ft	kip	kip				ASD	LRFD
		ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD					
W14x120	212	529	795	332	499	5.09	7.65	13.2	51.9	1380	171	257		
W18x97	211	526	791	328	494	9.41	14.1	9.36	30.4	1750	199	299		

$$\phi_b M_p = 791.0 \text{ FT. kips}$$

$$\phi_b M_r = 494 \text{ FT. kips}$$

$$L_r = 30.4'$$

For  $L_b > L_r$   $L_r = 30.40'$  @ LRF 10  
 Stress is  $F_{cr} \Rightarrow L_b = 38' > 30.40'$   
 $r_{ts} = 3.08$   $J = 5.86$   $C_b = 1$

$$F_{cr} = \frac{C_b \pi^2 E}{(L_b/r_{ts})^2} \sqrt{1 + 0.078 \frac{Jc}{S_x h_0} \left(\frac{L_b}{r_{ts}}\right)^2} \quad (\text{AISC Equation F2-4})$$

$$F_{cr} = \frac{1 (3.14155)^2 (29000)}{\left(\frac{(38)(12)}{3.08}\right)^2} \sqrt{1 + 0.078 \frac{(5.86)(1)}{(188)(17.7)} \left(\frac{(38)(12)}{3.08}\right)^2}$$

$$= 26.206 \text{ ksi}$$

$$M_n = F_{cr} S_x = 26.201 (188) = 4926.73 \text{ inch.kips}$$

$$\phi_b M_n = 0.9 (410.56) = 369.5 \text{ FT.kip} \quad \left\{ \begin{array}{l} / 12 \Rightarrow 410.56 \text{ FT.kips} \end{array} \right.$$

For  $L_b > L_r$

$$L_r = 30.40'$$

(b) ASD

Stress is  $F_{cr} \Rightarrow$

$$L_b = 38 > 30.40'$$

$$r_{ts} = 3.08$$

$$J = 5.86$$

$$C_b = 1$$

$$F_{cr} = \frac{C_b \pi^2 E}{(L_b/r_{ts})^2} \sqrt{1 + 0.078 \frac{Jc}{S_x h_0} \left(\frac{L_b}{r_{ts}}\right)^2}$$

(AISC Equation F2-4)

$$F_{cr} = \frac{1 (3.14155)^2 (29000)}{\left(\frac{(38)(12)}{3.08}\right)^2} \sqrt{1 + 0.078 \frac{(5.86)(1)}{(188)(17.7)} \left(\frac{(38)(12)}{3.08}\right)^2}$$

$$= 26.206 \text{ ksi}$$

$$M_n = F_{cr} S_x = 26.201 (188) = 4926.73 \text{ inch.kips}$$

$$\frac{1}{L_b} M_n = \frac{1}{1.67} (410.56) = 245.84 \text{ FT.kip} \quad \left. \begin{array}{l} 4926.73 \text{ inch.kips} \\ / 12 \Rightarrow 410.56 \text{ FT.kips} \end{array} \right\}$$

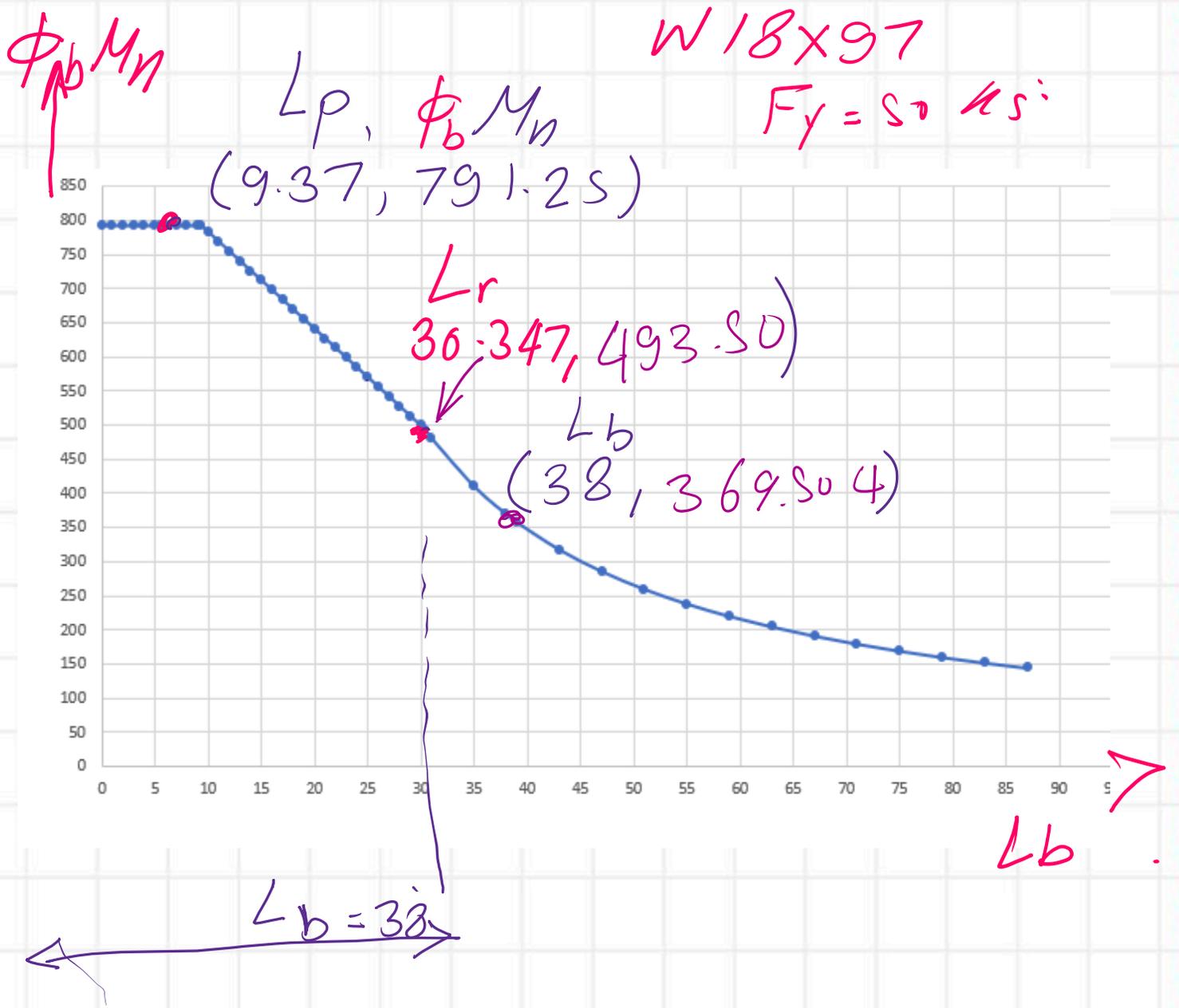
length of bracing-Ft	(ft)
0	
1	
2	
3	
4	
5	
5.58	
6	
7	
8	
9	
9.37	
10	

$\phi_b M_n$

Phi*Mn
791.25
791.25
791.25
791.25
791.25
791.25
791.25
791.25
791.25
791.25
791.25
791.25
791.25

28
29
30
30.347
31
35
38
39

527.481
513.315
499.158
493.497
480.519
410.031
369.504



$\frac{M_n}{\Omega}$

$F_y = 50 \text{ ksi}$

W 18 x 97

