

# Introduction to Local Buckling

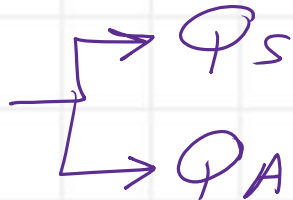
(a) Review of members with slender elements

(b) What are the chapters have a relation with Local Buckling

Chapter B Design requirements  $\rightarrow$  B4

Chapter E  $\rightarrow$  section E-7 (Design of Compression Members)

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2010



Limiting values for  $F_y$  Grades  
for slender / non slender  
members

## CHAPTER B

### DESIGN REQUIREMENTS

This chapter addresses general requirements for the analysis and design of steel structures applicable to all chapters of the specification.

The chapter is organized as follows:

- B1. General Provisions
- B2. Loads and Load Combinations
- B3. Design Basis
- B4. Member Properties →
- B5. Fabrication and Erection
- B6. Quality Control and Quality Assurance
- B7. Evaluation of Existing Structures

#### B4. MEMBER PROPERTIES

##### 1. Classification of Sections for Local Buckling

For compression, sections are classified as nonslender element or *slender-element sections*. For a nonslender element section, the width-to-thickness ratios of its compression elements shall not exceed  $\lambda_r$  from Table B4.1a. If the width-to-thickness ratio of any compression element exceeds  $\lambda_r$ , the section is a slender-element section.

For flexure, sections are classified as *compact*, *noncompact* or slender-element sections. For a section to qualify as compact, its flanges must be continuously connected to the web or webs and the width-to-thickness ratios of its compression elements shall not exceed the limiting width-to-thickness ratios,  $\lambda_p$ , from Table B4.1b. If the width-to-thickness ratio of one or more compression elements exceeds  $\lambda_p$ , but does not exceed  $\lambda_r$  from Table B4.1b, the section is noncompact. If the width-to-thickness ratio of any compression element exceeds  $\lambda_r$ , the section is a slender-element section.

Classification of Members slender → or non slender

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→ Slender  $> \lambda_r$   
non slender  $< \lambda_r$

## B4. MEMBER PROPERTIES

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flexure

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$\lambda \rightarrow \begin{cases} b_f/t_f \\ h_w/t_w \end{cases}$

Flange  $\rightarrow$  Unstiffened  
web  $\rightarrow$  stiffened

# DESIGN OF MEMBERS FOR COMPRESSION

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This chapter addresses members subject to axial compression through the centroidal axis.

The chapter is organized as follows:

- E1. General Provisions
- E2. Effective Length
- E3. Flexural Buckling of Members without Slender Elements
- E4. Torsional and Flexural-Torsional Buckling of Members without Slender Elements
- E5. Single Angle Compression Members
- E6. Built-Up Members
- E7. Members with Slender Elements

→ Section E-7

**User Note:** For cases not included in this chapter the following sections apply:

- H1 – H2 Members subject to combined axial compression and flexure
- H3 Members subject to axial compression and torsion
- I2 Composite axially loaded members
- J4.4 Compressive strength of connecting elements

## E7. MEMBERS WITH SLENDER ELEMENTS

Chapter E

This section applies to slender-element compression members, as defined in Section B4.1 for elements in uniform compression.

The *nominal compressive strength*,  $P_n$ , shall be the lowest value based on the applicable *limit states of flexural buckling, torsional buckling, and flexural-torsional buckling*.

$$P_n = F_{cr} A_g \quad (\text{E7-1})$$

The critical stress,  $F_{cr}$ , shall be determined as follows:

(a) When  $\frac{KL}{r} \leq 4.71 \sqrt{\frac{E}{QF_y}}$  (or  $\frac{QF_y}{F_e} \leq 2.25$ )

$$F_{cr} = Q \left[ 0.658 \frac{QF_y}{F_e} \right] F_y \quad (\text{E7-2})$$

*new Factor*  
*inelastic Column*

(b) When  $\frac{KL}{r} > 4.71 \sqrt{\frac{E}{QF_y}}$  (or  $\frac{QF_y}{F_e} > 2.25$ )

$$F_{cr} = 0.877 F_e \quad (\text{E7-3})$$

*Elastic Column*

spec-2010  
CM # 14  
 $\frac{KL}{r} \Rightarrow \frac{L_c}{r}$   
was replaced  
in specs-2016



$$\lambda_c^2 = \frac{F_y}{F_e}$$

$F_y$

E7-2

$$\lambda_c^2 = 2.25$$

E7-3

Critical stress, ksi

$$\frac{F_y}{2.25} = 0.44 F_y$$

$$F_e = \frac{\pi^2 E}{(\frac{KL}{r})^2} = \frac{F_y}{\lambda_c^2} \Rightarrow$$

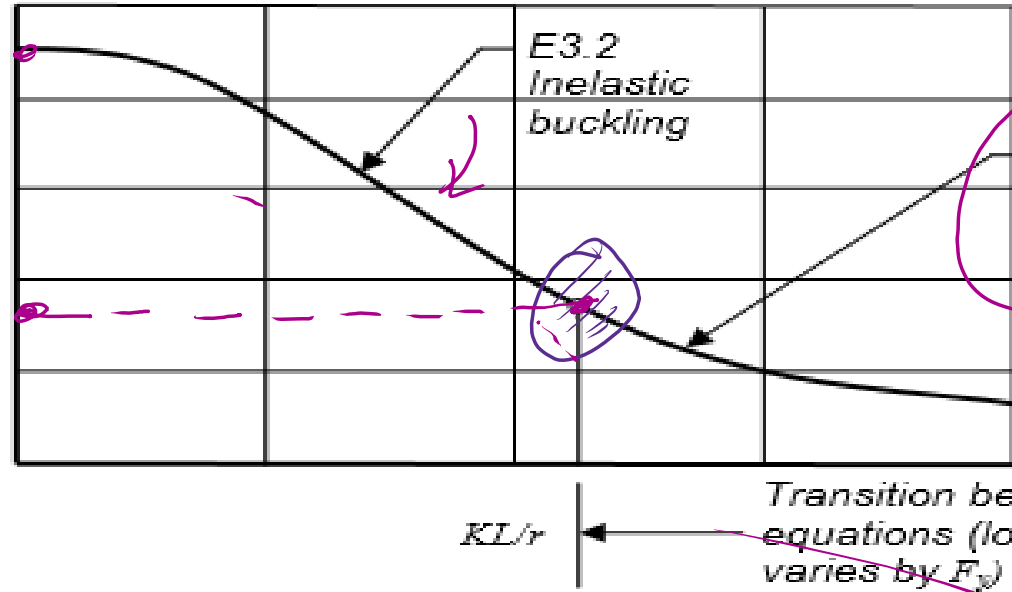


Figure E-1 Standard Column Curve

$$\left(\frac{KL}{r}\right)^2 = \frac{2.25 \pi^2 E}{F_y}$$

$$\frac{KL}{r} = 4.71 \sqrt{\frac{E}{F_y}}$$

TRANSITION POINT LIMITING VALUES OF $KL/r$		
$F_y$ ksi (MPa)	Limiting $KL/r$	$0.44 F_y$ ksi (MPa)
36 (248)	134	15.8 (109)
50 (345)	113	22.0 (152)
60 (414)	104	26.4 (182)
70 (483)	96	30.8 (212)

$$4.71 \sqrt{\frac{E}{F_y}} \Rightarrow 4.71 \sqrt{\frac{29000}{36}} = 133.68$$

B4 → 1a

## Chapter B

→ Flanges

### 1a. Unstiffened Elements

→ Unstiffened

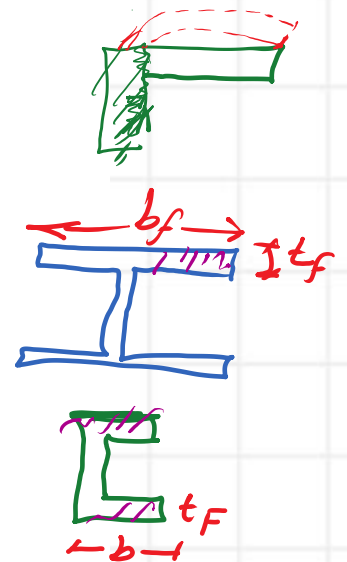
For *unstiffened elements* supported along only one edge parallel to the direction of the compression force, the width shall be taken as follows:

- (a) For flanges of I-shaped members and tees, the width,  $b$ , is one-half the full-flange width,  $b_f$ .
- (b) For legs of angles and flanges of channels and zees, the width,  $b$ , is the full *nominal dimension*.
- (c) For plates, the width,  $b$ , is the distance from the free edge to the first row of fasteners or line of welds.
- (d) For stems of tees,  $d$  is taken as the full nominal depth of the section.

What are the Unstiffened items

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AMERICAN INSTITUTE OF STEEL CONSTRUCTION

Unstiffened



**User Note:** Refer to Table B4.1 for the graphic representation of unstiffened element dimensions.

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$\Rightarrow$  CM # 14 16.1-40/41 Section E

1. **Slender Unstiffened Elements,  $Q_s$**

The reduction factor,  $Q_s$ , for slender *unstiffened elements* is defined as follows:

(a) For flanges, angles and plates projecting from rolled *columns* or other compression members:

(i) When  $\frac{b}{t} \leq 0.56 \sqrt{\frac{E}{F_y}}$

$$Q_s = 1.0 \quad (\text{E7-4})$$

(ii) When  $0.56 \sqrt{\frac{E}{F_y}} < \frac{b}{t} < 1.03 \sqrt{\frac{E}{F_y}}$

$$Q_s = 1.415 - 0.74 \left( \frac{b}{t} \right) \sqrt{\frac{F_y}{E}} \quad (\text{E7-5})$$

(iii) When  $\frac{b}{t} \geq 1.03 \sqrt{\frac{E}{F_y}}$





$$Q_s = \frac{0.69 E}{F_y \left( \frac{b}{t} \right)^2} \quad (\text{E7-6})$$

*Qs Equations*



**TABLE B4.1a**  
**Width-to-Thickness Ratios: Compression Elements**  
**Members Subject to Axial Compression**

axial  
Compression

Case	Description of Element	Width-to-Thickness Ratio	Limiting Width-to-Thickness Ratio $\lambda_c$ (nonslender/slender)	Examples
Unslendered Elements	1 Flanges of rolled I-shaped sections, plates projecting from rolled I-shaped sections; outstanding legs of pairs of angles connected with continuous contact, flanges of channels, and flanges of tees	$b/t$	$0.56\sqrt{\frac{E}{F_y}}$	
	2 Flanges of built-up I-shaped sections and plates or angle legs projecting from built-up I-shaped sections	$b/t$	$0.64\sqrt{\frac{K_c E}{F_y}}$	
	3 Legs of single angles, legs of double angles with separators, and all other unslendered elements	$b/t$	$0.45\sqrt{\frac{E}{F_y}}$	
	4 Stems of tees	$d/t$	$0.75\sqrt{\frac{E}{F_y}}$	 T

Flanges of W  
 $\Rightarrow 0.56\sqrt{\frac{E}{F_y}}$

Built up  
 $\rightarrow 0.64\sqrt{\frac{K_c E}{F_y}}$

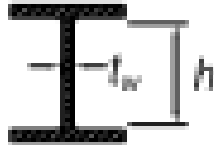
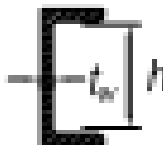
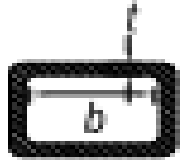
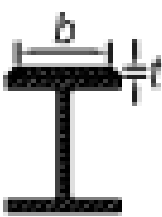
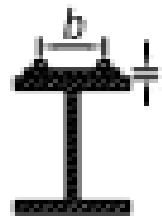
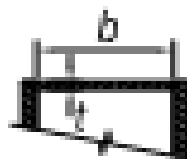
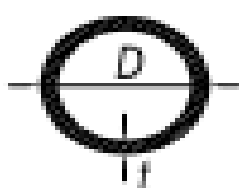
Legs  
 $\rightarrow 0.45\sqrt{\frac{E}{F_y}}$

$\rightarrow 0.75\sqrt{\frac{E}{F_y}}$

B4.1a

stiffened Elements

CM # 14  
# 2010

Stiffened Elements	5	Webs of doubly-symmetric I-shaped sections and channels	$h/t_w$	$1.49 \sqrt{\frac{E}{F_y}}$	 	$h/t_w$
	6	Walls of rectangular HSS and boxes of uniform thickness	$b/t$	$1.40 \sqrt{\frac{E}{F_y}}$		$b/t$
	7	Flange cover plates and diaphragm plates between lines of fasteners or welds	$b/t$	$1.40 \sqrt{\frac{E}{F_y}}$	 	$b/t$
	8	All other stiffened elements	$b/t$	$1.49 \sqrt{\frac{E}{F_y}}$		$b/t$
	9	Round HSS	$D/t$	$0.11 \frac{E}{F_y}$		$D/t$

## 1b. Stiffened Elements

## Sec B-3

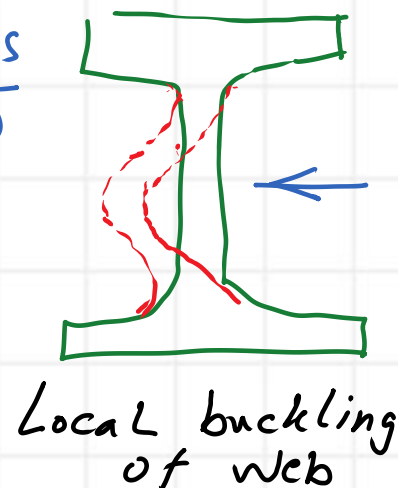
For *stiffened elements* supported along two edges parallel to the direction of the compression force, the width shall be taken as follows:

- (a) For webs of rolled or *formed sections*,  $h$  is the clear distance between flanges less the fillet or corner radius at each flange;  $h_c$  is twice the distance from the center of gravity to the inside face of the compression flange less the fillet or corner radius.

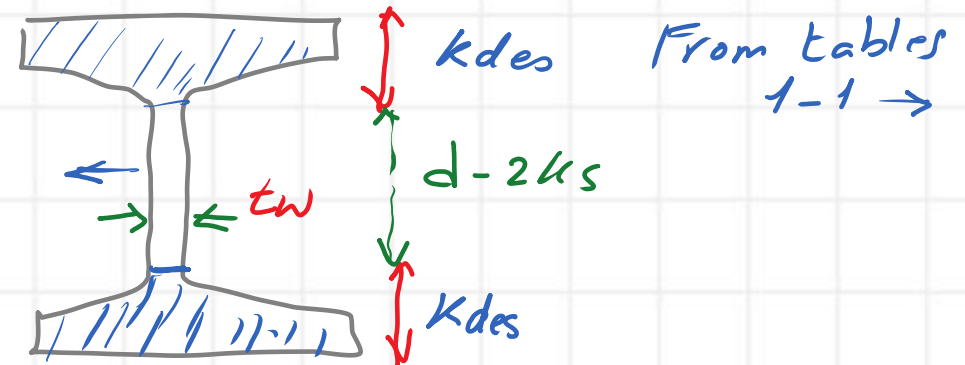
$$\lambda = \frac{d - 2k_s}{t_w}$$

$$\lambda_r = 1.49 \sqrt{\frac{F_y}{E}}$$

Item -5  
s stiffened



Stiffened web



Prepared by Eng. Maged Kamel.

$P_n$

16.1  $\rightarrow$  43

## 2. Slender Stiffened Elements, $Q_a$

The reduction factor,  $Q_a$ , for slender *stiffened elements* is defined as follows:

$$Q_a = \frac{A_e}{A_g} \quad (\text{E7-16})$$

where

$A_g$  = gross cross-sectional area of member, in.<sup>2</sup> (mm<sup>2</sup>)

$A_e$  = summation of the effective areas of the cross section based on the reduced *effective width*,  $b_e$ , in.<sup>2</sup> (mm<sup>2</sup>)

The reduced effective width,  $b_e$ , is determined as follows:

- (a) For uniformly compressed slender elements, with  $\frac{b}{t} \geq 1.49 \sqrt{\frac{E}{f}}$ , except flanges of square and rectangular sections of uniform thickness:

$$b_e = 1.92t \sqrt{\frac{E}{f}} \left[ 1 - \frac{0.34}{(b/t)} \sqrt{\frac{E}{f}} \right] \leq b \quad (\text{E7-17})$$

where

$f$  is taken as  $F_{cr}$  with  $F_{cr}$  calculated based on  $Q = 1.0$

- (b) For flanges of square and rectangular *slender-element sections* of uniform thickness with  $\frac{b}{t} \geq 1.40 \sqrt{\frac{E}{f}}$ :

$$b_e = 1.92t \sqrt{\frac{E}{f}} \left[ 1 - \frac{0.38}{(b/t)} \sqrt{\frac{E}{f}} \right] \leq b \quad (\text{E7-18})$$

where

$f = P_n/A_e$

**User Note:** In lieu of calculating  $f = P_n/A_e$ , which requires iteration,  $f$  may be taken equal to  $F_y$ . This will result in a slightly conservative estimate of *column available strength*.

