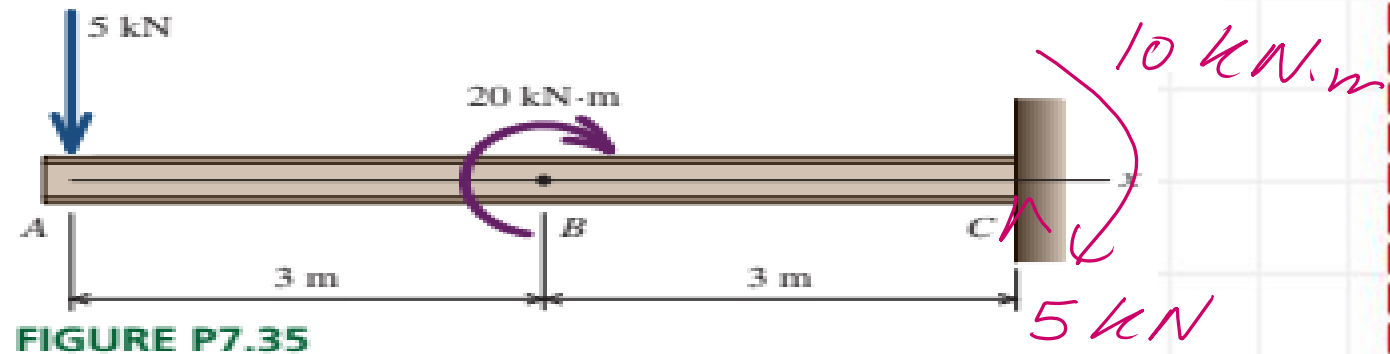
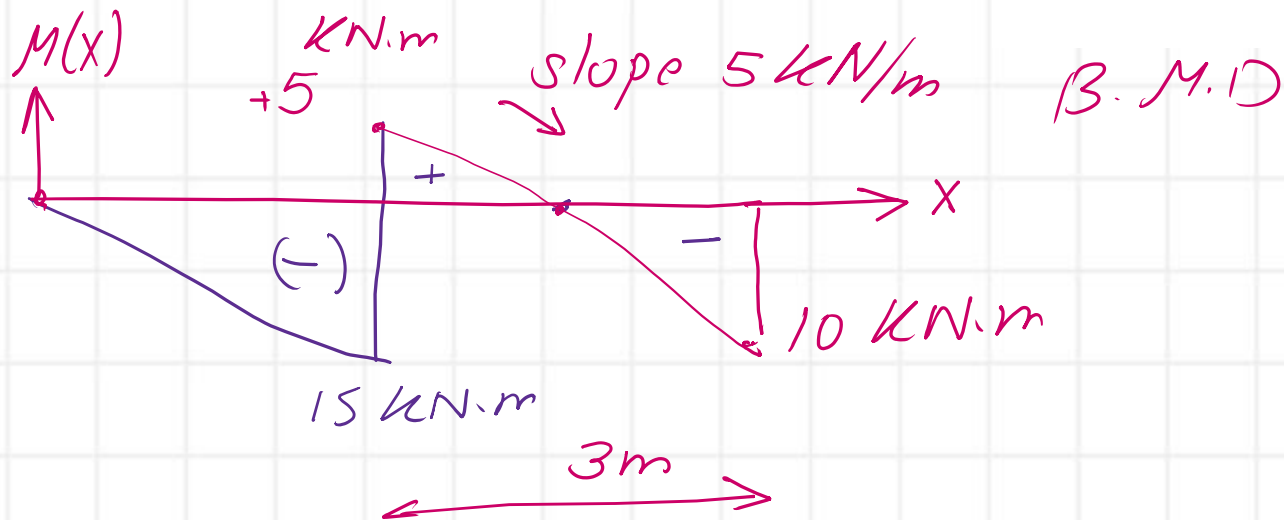
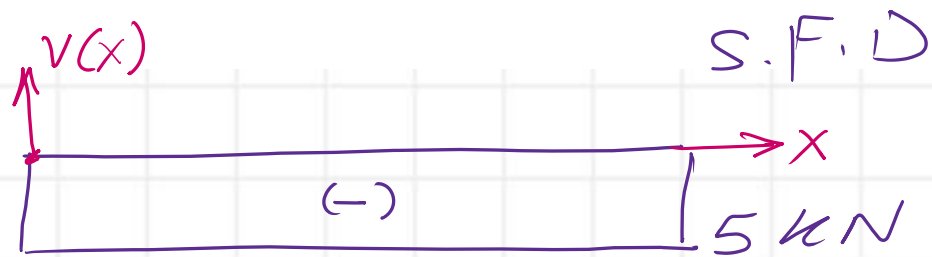


P7.32–P7.42 For the beams and loadings shown in Figures P7.32–P7.42,

- use discontinuity functions to write the expression for $w(x)$; include the beam reactions in this expression.
- integrate $w(x)$ twice to determine $V(x)$ and $M(x)$.
- use $V(x)$ and $M(x)$ to plot the shear-force and bending-moment diagrams.



Prepared by Eng. Maged Kamel.

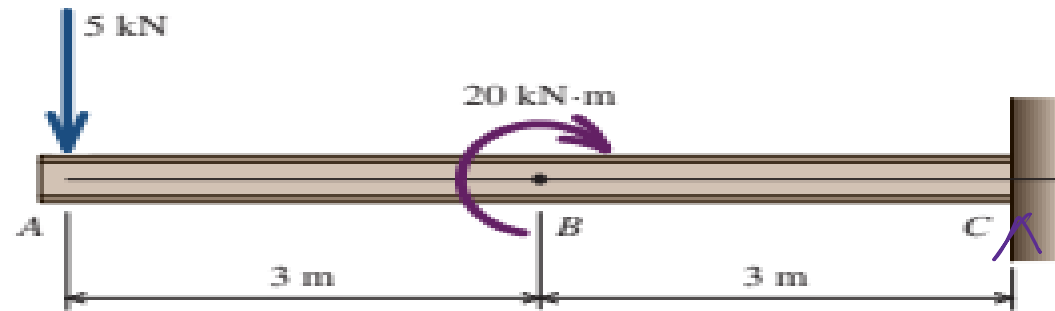


FIGURE P7.35

10 kN-m

step in $x = 3$

For moment
5 kN has no effect

$$V(x) = -5 \langle x-0 \rangle^0 + 20 \langle x-3 \rangle^{-1} + 5 \langle x-6 \rangle^0 + 10 \langle x-6 \rangle^{-1}$$

$$= \text{IF}(\text{AND}(0 \leq A17, A17 \leq 3), -5, \text{IF}(\text{AND}(3 < A17, A17 \leq 6), -$$

$$5, 0)) \quad A_{14} \Rightarrow x \geq 0 \quad V(x) = -5(1) = -5 \text{ kN}$$

$$\rightarrow A_{15} \Rightarrow x = 1 \quad V(x) = -5(1) = -5 \text{ kN}$$

$$x \leq 3 \quad V(x) = -5(1) = -5 \text{ kN}$$

$$= \text{IF}(\text{AND}(0 \leq A18, A18 < 3), -$$

$$5, \text{IF}(\text{AND}(3 \leq A18, A18 \leq 6), -5, 0))$$

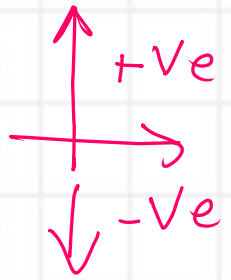
$$A_{18} \Rightarrow x > 3$$

$$V(x) = -5(1) = -5 \text{ kN}$$

$$A_{21} \rightarrow \leq 6$$

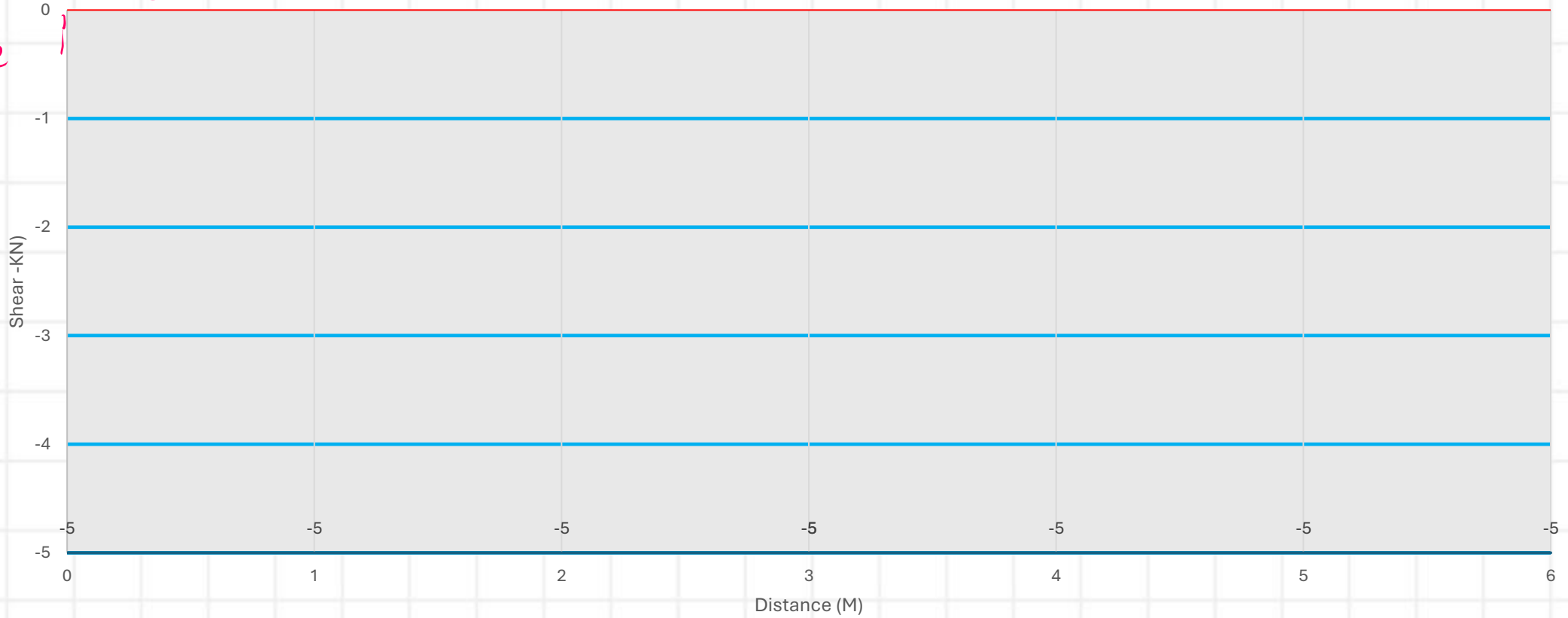
$$V(x) = -5(1) = -5 \text{ kN}$$

	A	B	C
Distance x (m)	Shear V(x)-kN	Moment in kN-M	
0	-5	0	
1	-5	-5	
2	-5	-10	
3	-5	-15	
3	-5	5	
4	-5	0	
5	-5	-5	
6	-5	-10	



Datum

Shear Diagram



=IF(AND(0<=A14,A14<3),-5,IF(AND(3<=A14,A14<=6),-5,0))

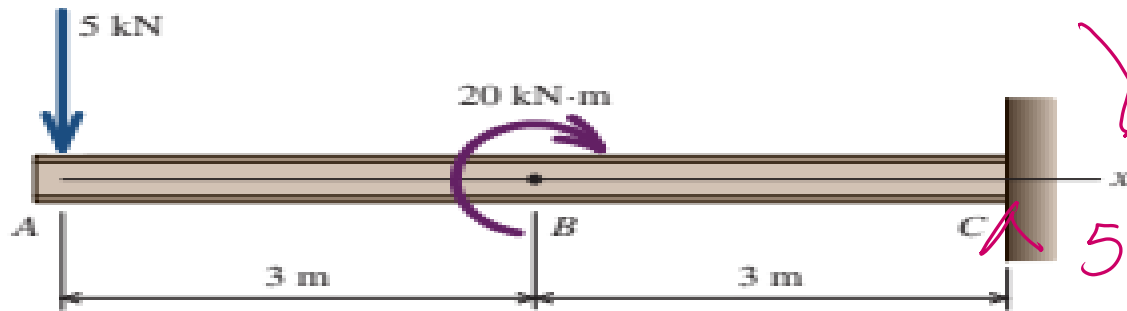


FIGURE P7.35

10 kN·m

step in $x = 3$

5 kN

For moment

$x > 6$ m

$$M(x) = -5 \langle x-0 \rangle^1 + 20 \langle x-3 \rangle^0 + 5 \langle x-6 \rangle^1 + 10 \langle x-6 \rangle^0$$

	A	B	C
Distance			
x (m)			
0			
1			
2			
3			
3			
4			
5			
6			

M

$$= \text{IF}(\text{AND}(0 \leq A17, A17 \leq 3), -5 \cdot A17, \text{IF}(\text{AND}(3 < A17, A17 \leq 6), -5 \cdot A17 + 20 \cdot 1, 0))$$

$$x \geq 0 \Rightarrow M = 0 \text{ kN} \cdot \text{m}$$

$$x \leq 3 \rightarrow M = -5x = -5(3) = -15 \text{ kN} \cdot \text{m}$$

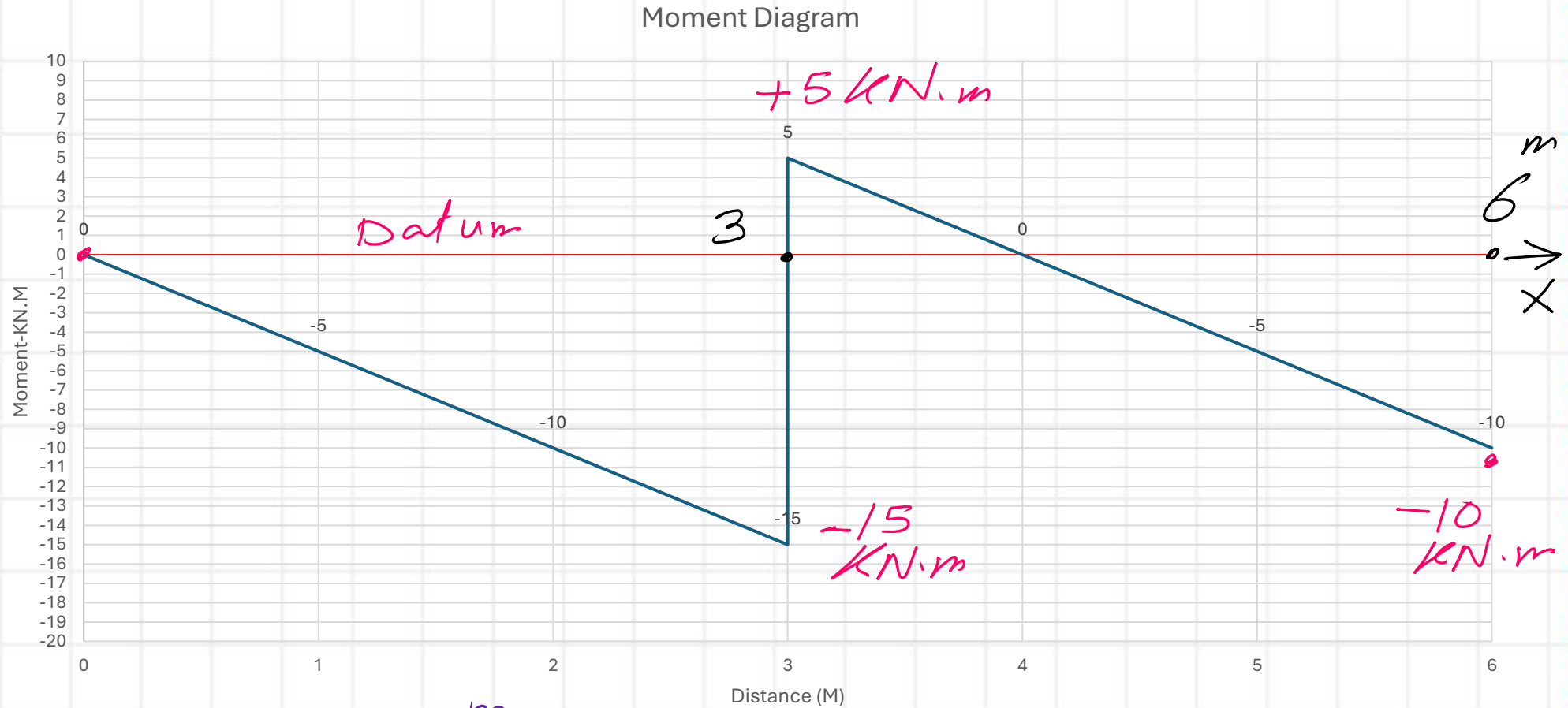
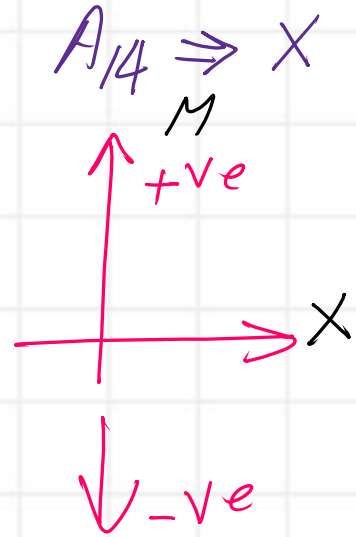
$$= \text{IF}(\text{AND}(0 \leq A18, A18 < 3), -5 \cdot A18, \text{IF}(\text{AND}(3 \leq A18, A18 \leq 6), -5 \cdot A18 + 20 \cdot 1, 0))$$

$$x > 3 \text{ m} \leq 6 \text{ m}$$

$$M = -5(3) + 20(2) = +5 \text{ kN} \cdot \text{m}$$

$$= -5(6) + 20(3) = -10$$

$$=IF(AND(0 \leq A14, A14 \leq 3), -5 * A14, IF(AND(3 < A14, A14 \leq 6), -5 * A14 + 20, 0))$$



$3 \xrightarrow{m} 6$

Equation if and

$$=IF(AND(0 \leq A18, A18 < 3), -5 * A18, IF(AND(3 \leq A18, A18 \leq 6), -5 * A18 + 20, 0))$$