## From: Pivoting for LU Factorization Matthew W. Reid

A permutation matrix is the identity matrix with interchanged rows.

When these matrices are multiplied by another matrix, they swap the rows or columns of the matrix.

Left multiplication by a permutation matrix will result in the swapping of rows while right multiplication will swap Columns.

Prepared by Eng. Maged Kamel.

Permutation Matrix 2x2 Identity matrix

[0] if We [ab] matrix

[0] multiply [cd] matrix Then  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$   $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$  =  $\begin{bmatrix} a+0 & b+0 \\ 0+c & o+d \end{bmatrix}$  =  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ We will not have in Change in Matrix A But if we want to change the rows of Matrix A For instance Swap of R2 we need Permutation matrix

 $a_{11} = a$ a 21 - C To this 2x2 Matrix to Change the arrangement of row-1- row-2 and vice Verse Use Permutation matrix denoted by P (b) Movin an an 21 & arr 2012 Use P Matrix From the Left of a matric

matric

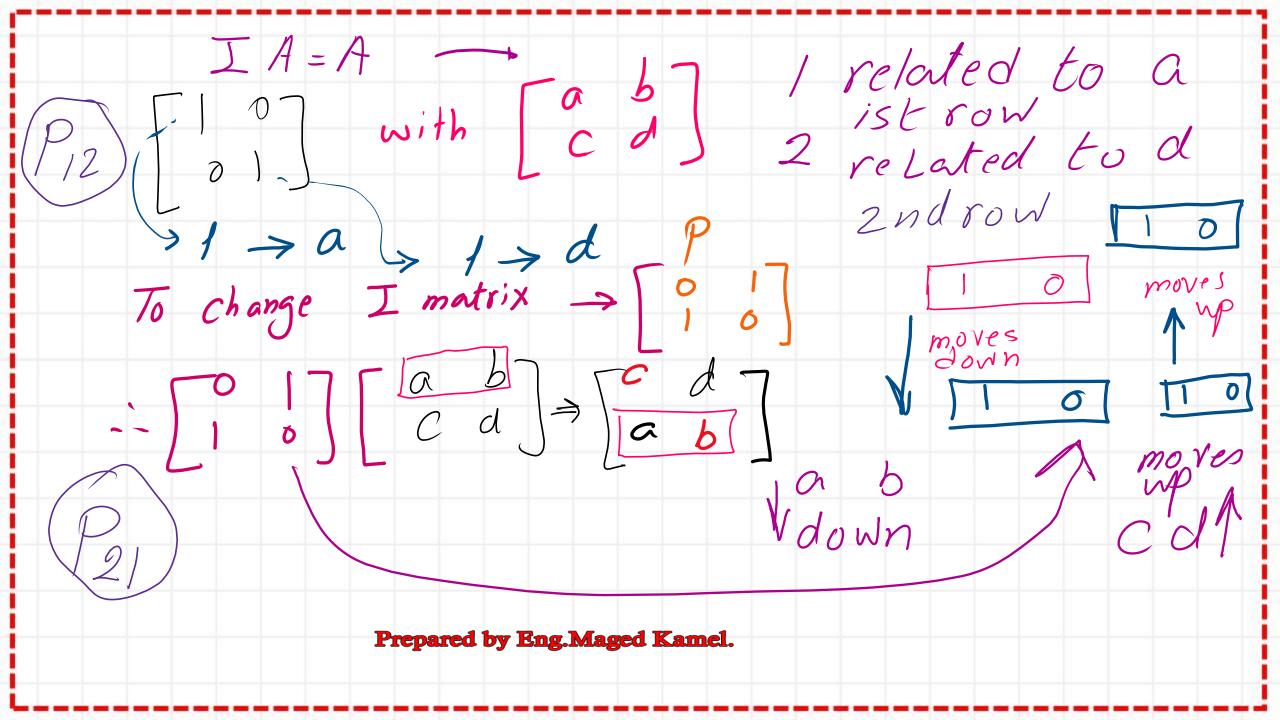
o 17 move ist frow > 2nd row

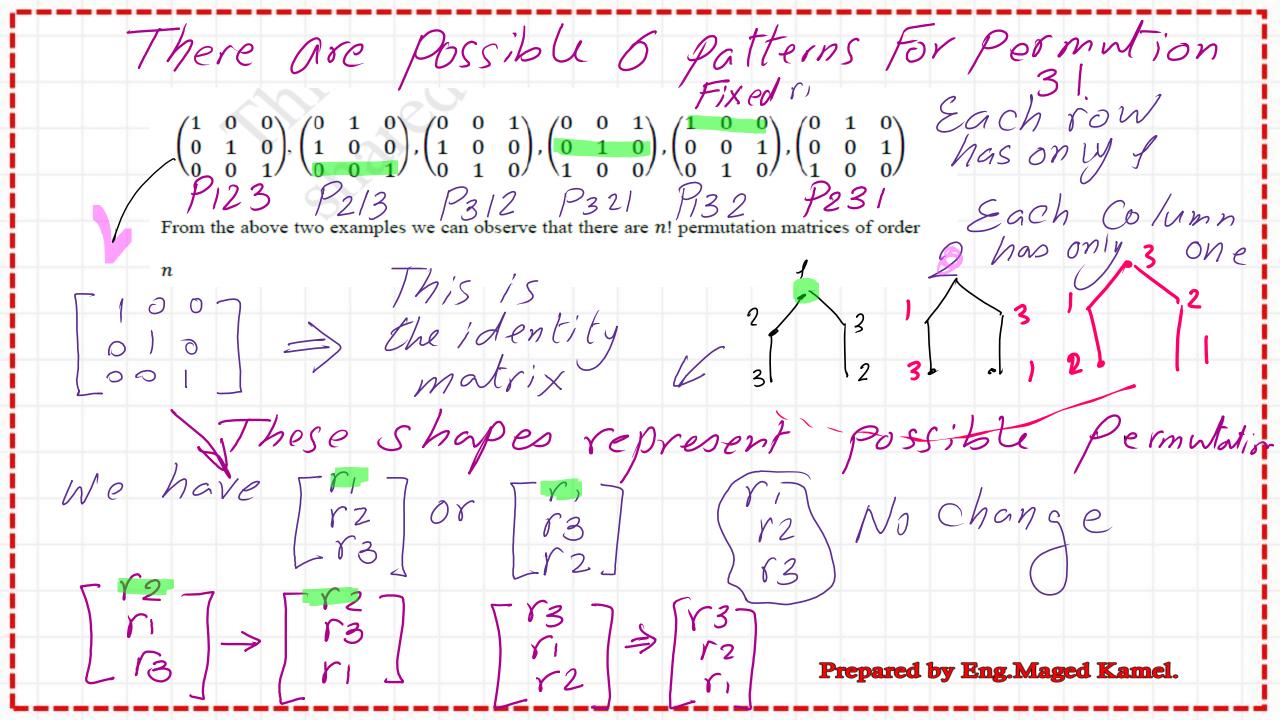
and vice

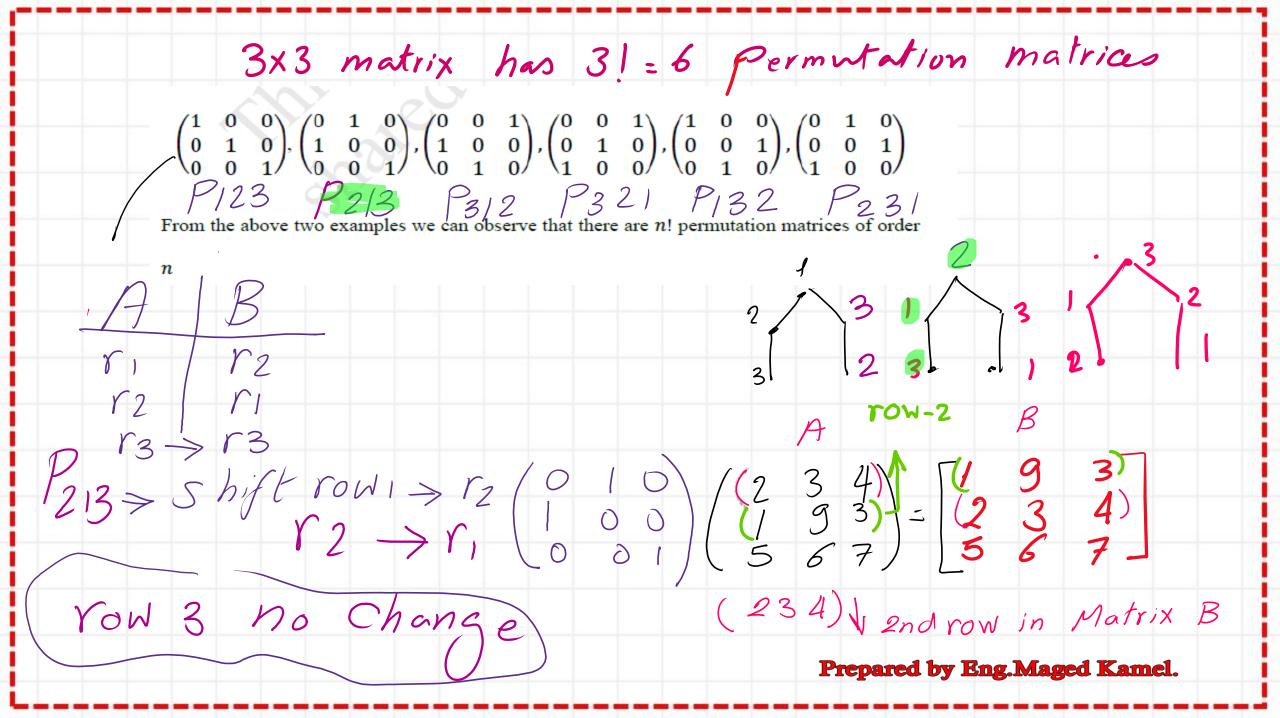
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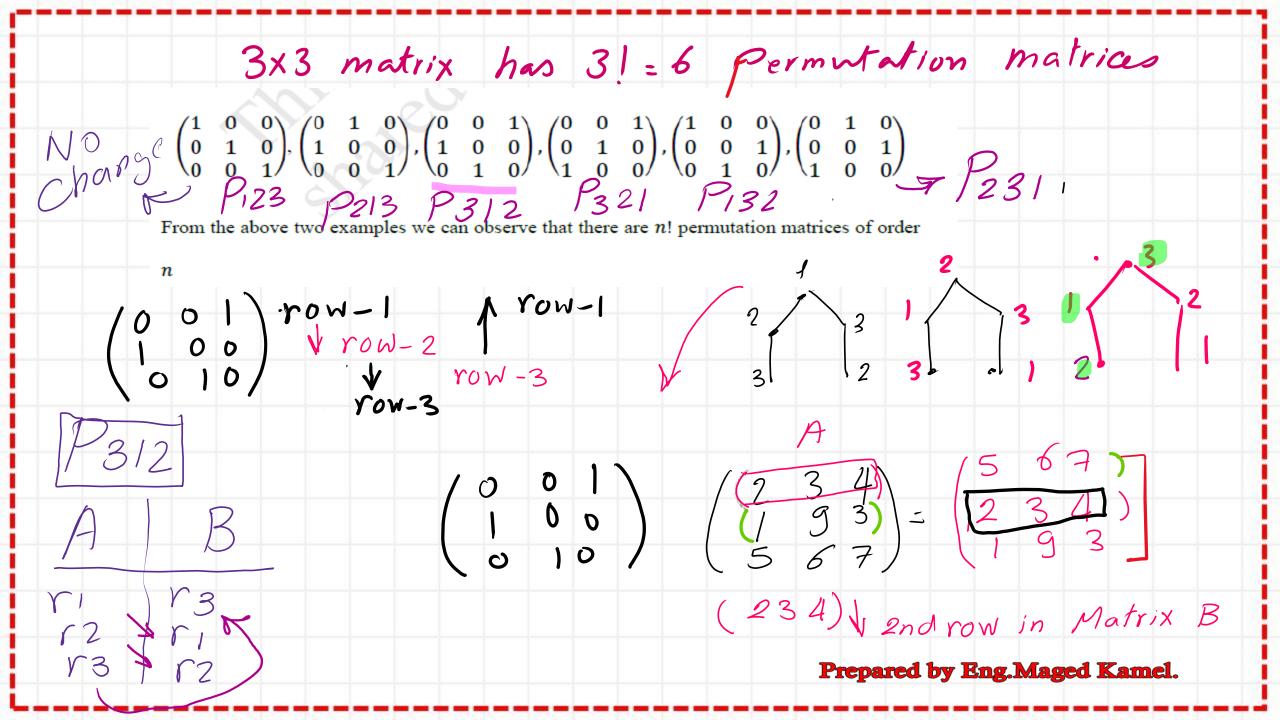
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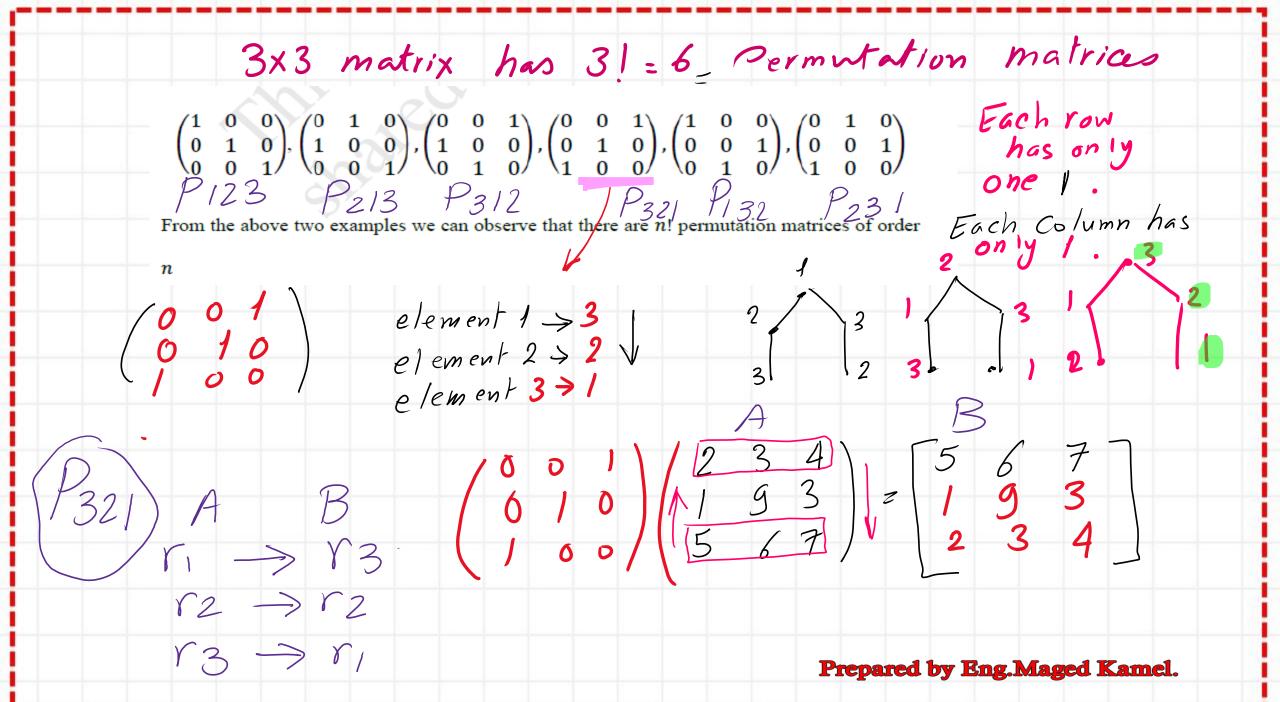
How Can We Change the arrangement of Glumns for a 2x2 matrix? But if we want to change Column arrangement instead of [ab] = [bac] We will multiply by Permutation Matrix  $\begin{bmatrix} a & b \\ C & d \end{bmatrix} * \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} b & a \\ d & C \end{bmatrix}$  2 = 2H Matrix A' P12 P21 mulliply from risht

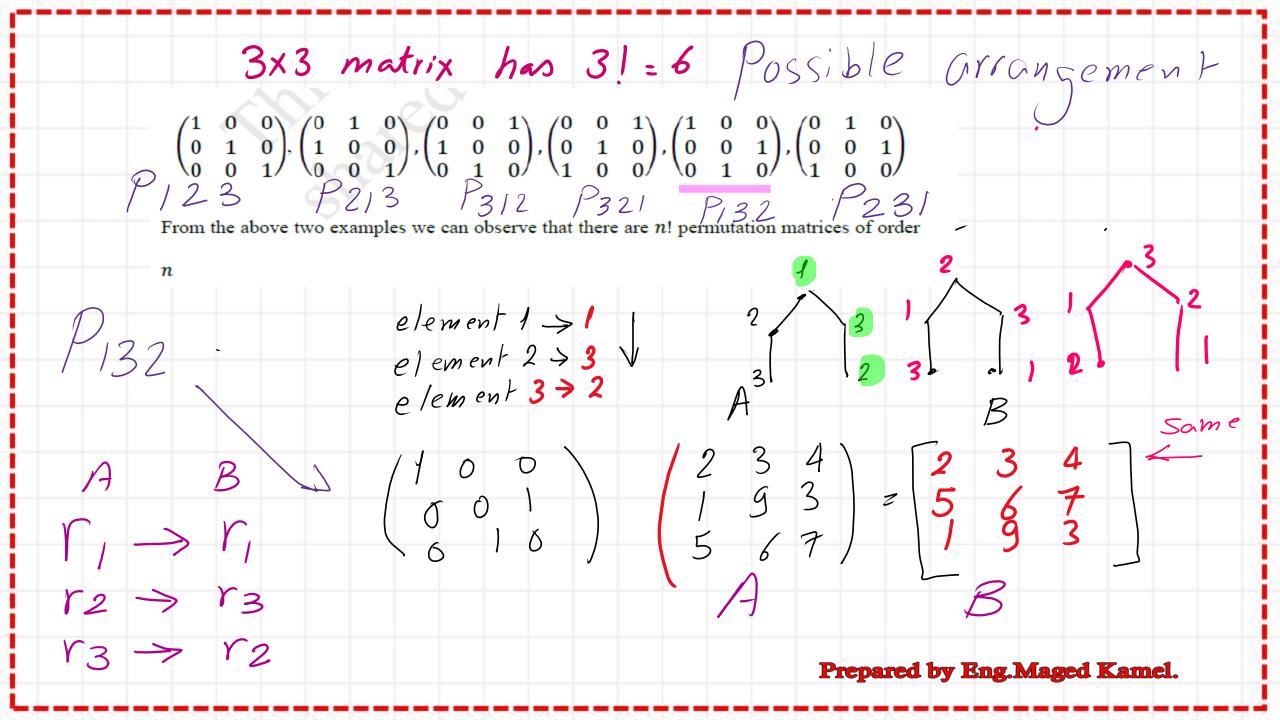


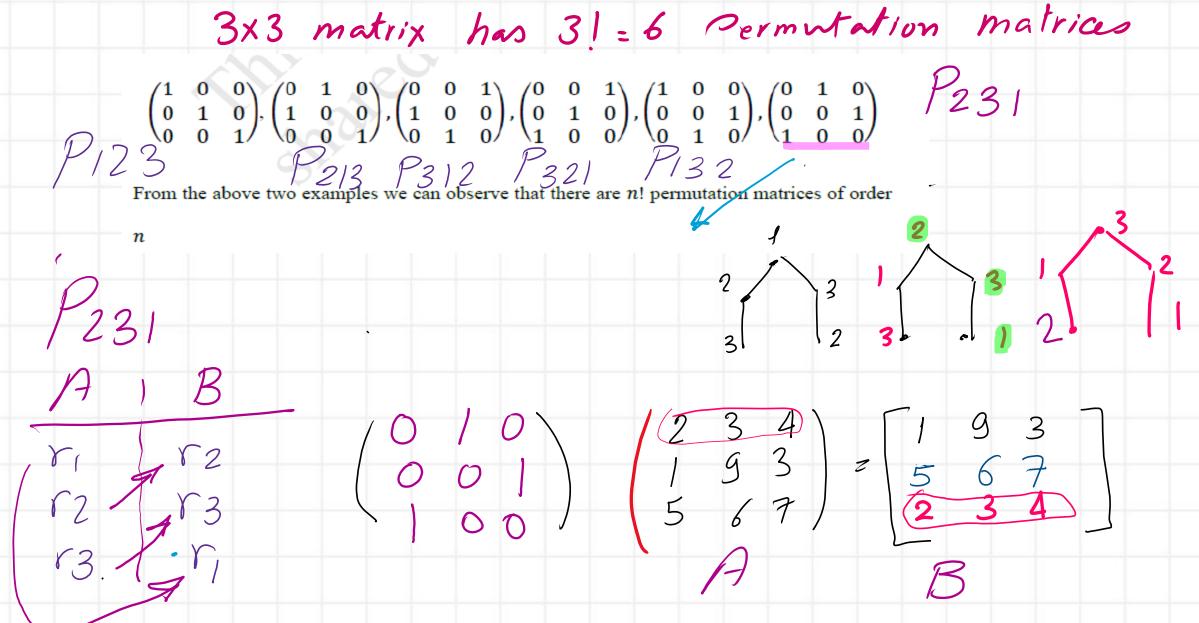




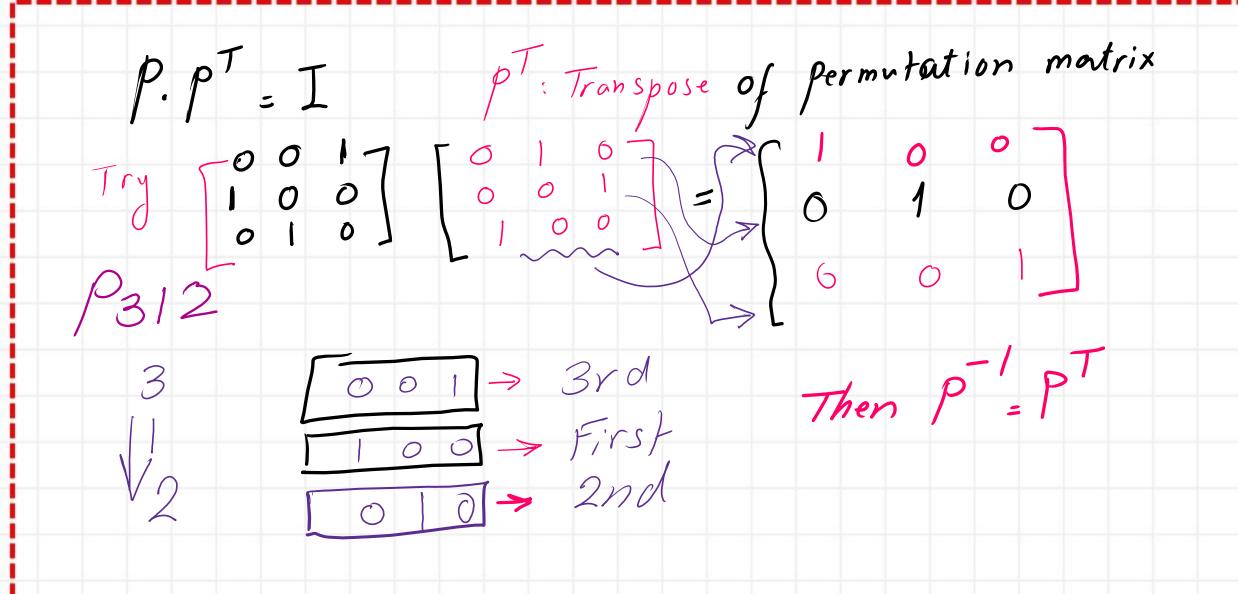








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P: Transpose of permutation matrix

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