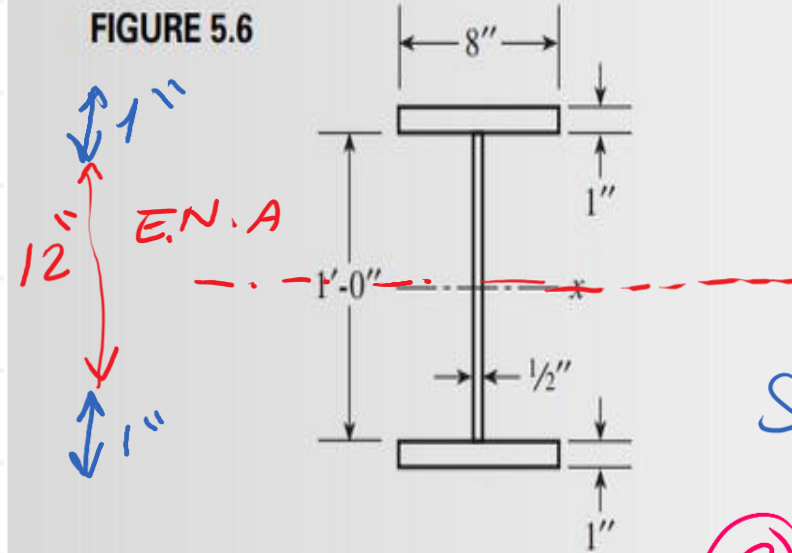


EXAMPLE 5.1

From Prof. William Segui's book

For the built-up shape shown in Figure 5.6, determine (a) the elastic section modulus S and the yield moment M_y , and (b) the plastic section modulus Z and the plastic moment M_p . Bending is about the x -axis, and the steel is A572 Grade 50.

@ Part a
Elastic section modulus



① Due to symmetry E.N.A will be in middle of the Built-up section

$$S_x = \frac{I}{y_{\max}} \quad \text{our } y_{\max} = (12 + 1 + 1) \cdot 0.50 = 7''$$

② I_x can be estimated for half of the Built up section and then multiply by 2.

③ We can estimate I_x as for a big Rectangle and deduct void rectangle I_x value.

Prepared by Eng. Maged Kamel.

EXAMPLE 5.1

P-2

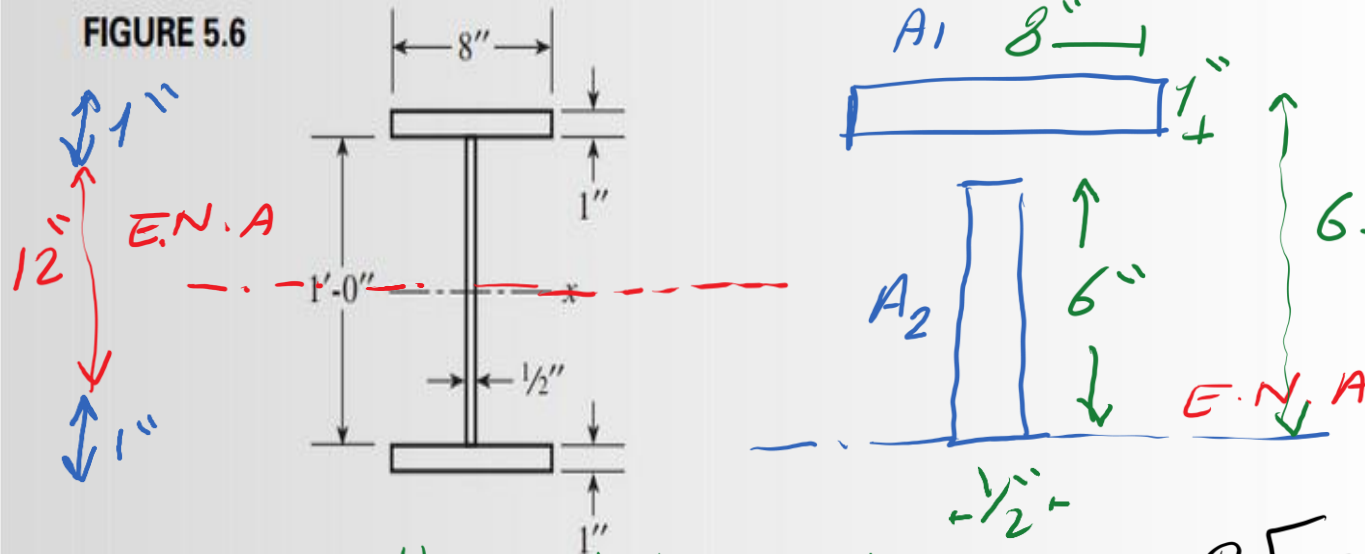
Fro Prof. William SeGvi's book

For the built-up shape shown in Figure 5.6, determine (a) the elastic section modulus S and the yield moment M_y , and (b) the plastic section modulus Z and the plastic moment M_p . Bending is about the x -axis, and the steel is A572 Grade 50.

$I_{x1} = I_{xcg} + A_1 \bar{y}_1^2$
 $= \frac{8(1)^3}{12} + (8)(6.5)^2$
 $\Rightarrow 338.666 \text{ inch}^4$

$A_2 - I_{x2}$
 $= \left(\frac{1}{2}\right) \frac{(6)^3}{12} + (3)(3)^2 = 36 \text{ inch}^4$

FIGURE 5.6



I_x For the whole section $\Rightarrow 2 [338.666 + 36] = 749.333 \text{ inch}^4$

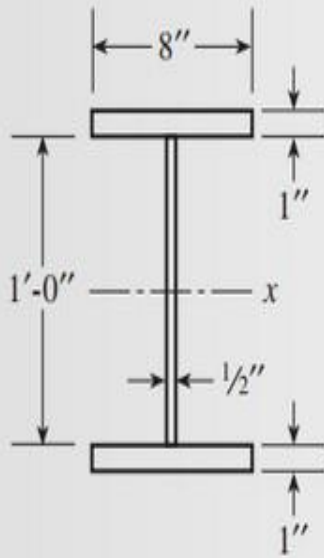
$S_x = \frac{I_x}{y} = \frac{I_x}{h/2} = \frac{2(749.333)}{14} = 107.05 \text{ inch}^3$

Prepared by Eng. Maged Kamel.

EXAMPLE 5.1

For the built-up shape shown in Figure 5.6, determine (a) the elastic section modulus S and the yield moment M_y , and (b) the plastic section modulus Z and the plastic moment M_p . Bending is about the x -axis, and the steel is A572 Grade 50.

FIGURE 5.6



Page 3

M_y can be estimated

$$F_y = 50 \text{ ksi}$$

Yielding Moment Directly From S_x value

$$S_x = \frac{I_x}{y}, \text{ but } f = \frac{M_y}{I_x} \cdot y = \frac{M_y}{S_x}$$

$$F = F_y = 50 \text{ ksi} \quad M_y = S_x \cdot f_y = 107.05 (50)$$

$$M_y = 5352.6 \text{ k. inch. Lb} \left(\frac{\text{Ft}}{12 \text{ inch}} \right) \text{ inch}^3 \left(\frac{\text{k Lb}}{\text{inch}^2} \right)$$

$$= 446.05 \text{ FT. kips}$$

$$M_y = 446 \text{ FT. kips}$$

EXAMPLE 5.1

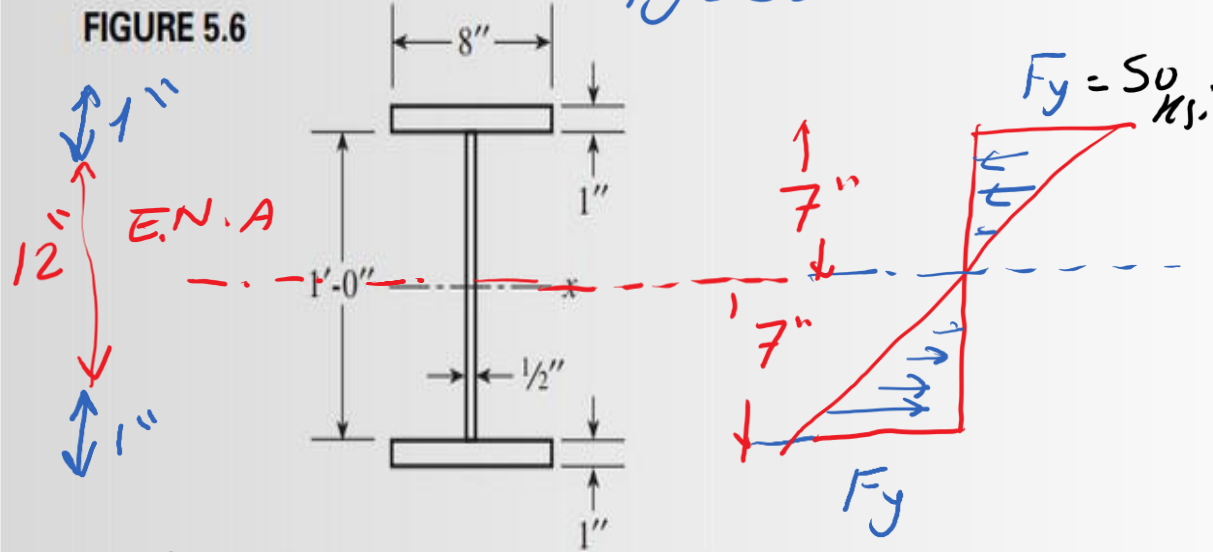
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From Prof. William Segui's book

S_x : elastic section Modulus

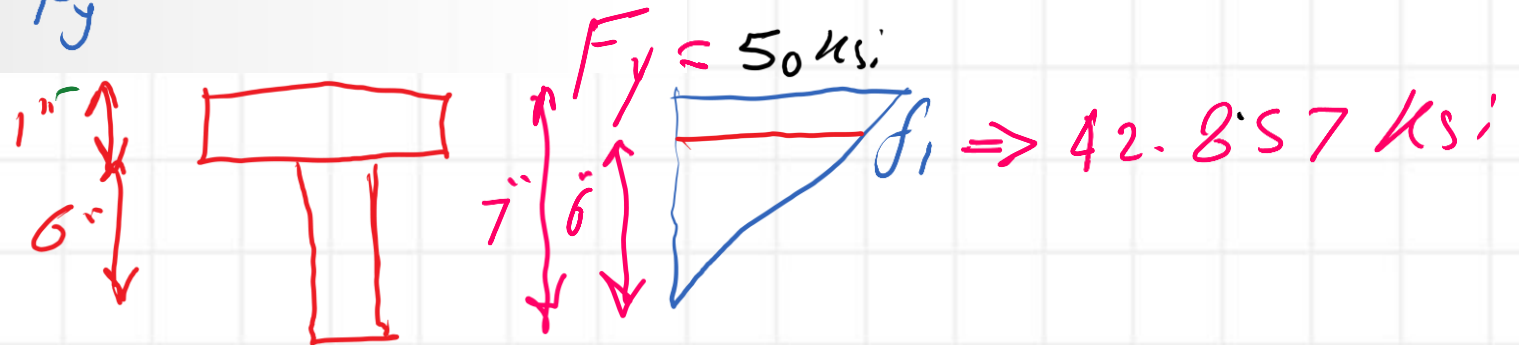
P. 4

if we wish to calculate M_y from first principles it might take additional calculations as follows



f_1 at the junction

$$= \left(\frac{6}{7}\right)(50) = 42.857 \text{ ksi}$$

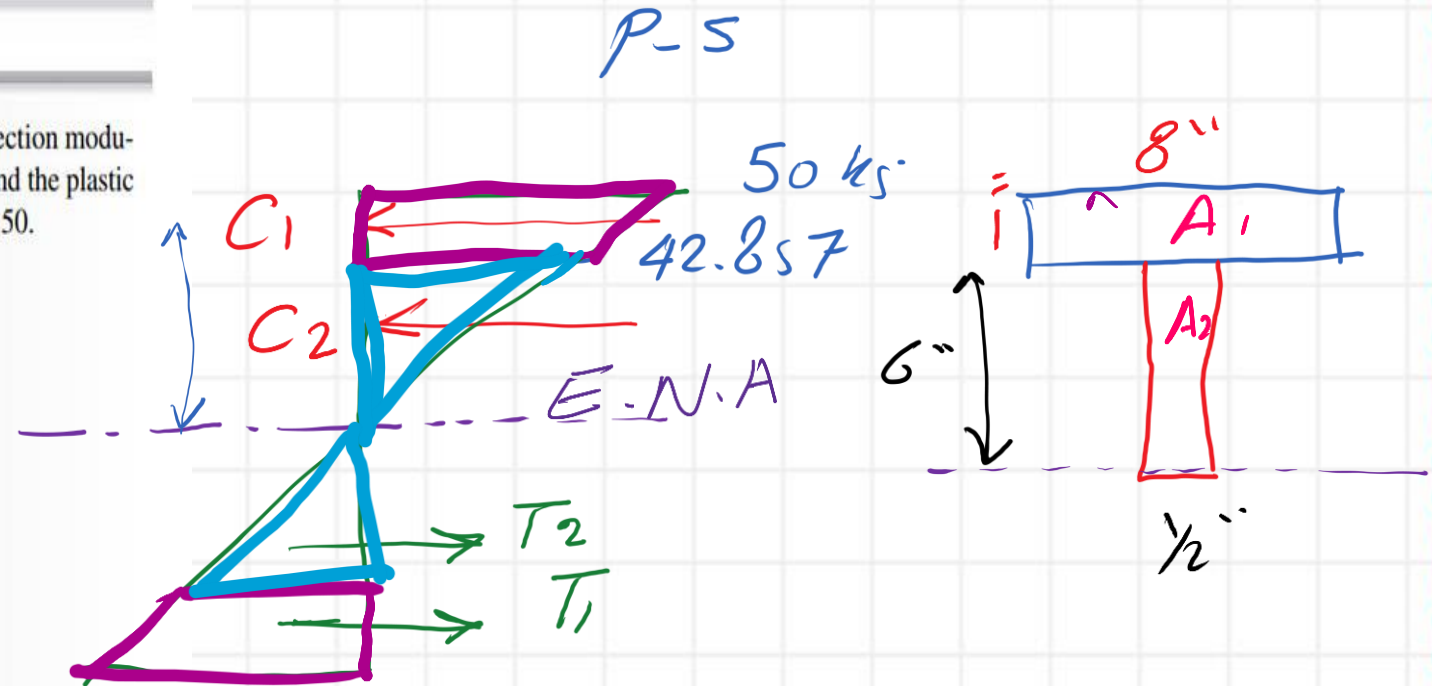
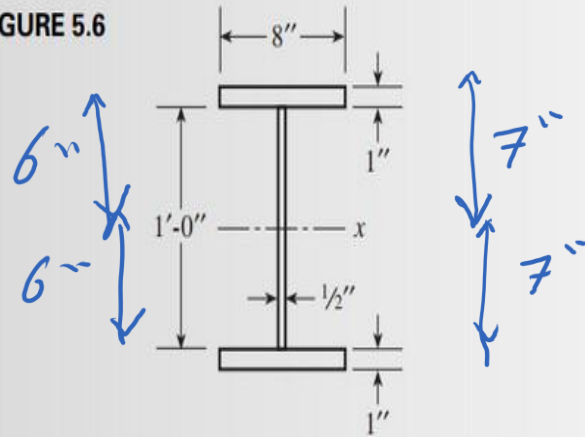


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EXAMPLE 5.1

For the built-up shape shown in Figure 5.6, determine (a) the elastic section modulus S and the yield moment M_y , and (b) the plastic section modulus Z and the plastic moment M_p . Bending is about the x -axis, and the steel is A572 Grade 50.

FIGURE 5.6



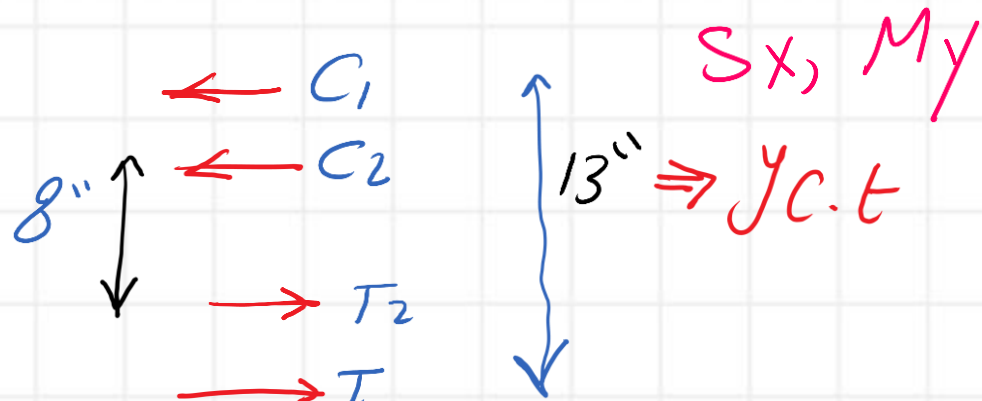
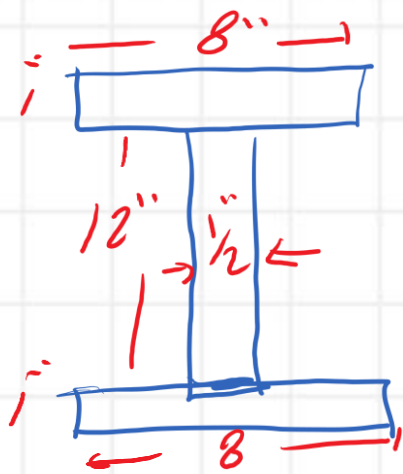
$$\text{Compression Force } C_1 = \frac{1}{2} (42.857 + 50) [8](1) = 371.428 \text{ kips}$$

$$\text{Arm of } C_1 \Rightarrow E.N.A. = 7 - \frac{1}{2}(1) = 6\frac{1}{2}''$$

$$\text{while } C_2 = \frac{1}{2} (42.857) \left(\frac{6}{2}\right) = 64.285 \text{ kips}$$

$$C_2 \text{ arm to E.N.A.} = \frac{2}{3}(6) = 4''$$

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P-6

Part (a)

List Each Force and the Relative arm y_{c-t}
From Compression to Tension.

Forces	value	y_{c-t}	M_y
C_1	371.428	13"	4828.56
C_2	64.285	8"	514.28

5342.84 inch kips

$$M_y = 5342.84 \text{ inch.kips} \left(\frac{\text{Ft}}{12 \text{ inch}} \right) = 445.23 \text{ Ft.kips}$$

close to the previous M_y value by S_x

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